

# Object-Oriented Modelling from a Control Engineer's Perspective: Past, Present, and Future

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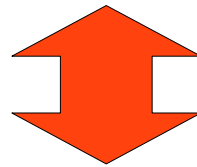
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Object-Oriented Modelling Tools



Computer-Aided Control  
System Design Tools

# Requirements for control-oriented physical modelling

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- *Modularity*
  - modular modelling
  - physical, a-causal interfaces
  - hierarchical system decomposition
- *Flexibility*
  - appropriate level of detail
  - replaceable component and sub-system models
- *Reusability*
  - do not reinvent the wheel
  - capitalize on past modelling investment
- *Generality*
  - multi-domain system modelling
- *Extensibility / Customizability*
  - overcome the “component not available” syndrome
  - including proprietary information
- *Plant-Control Integration*
  - closed-loop Modelica model
  - Modelica plant + external controller (Simulink, HIL, etc)

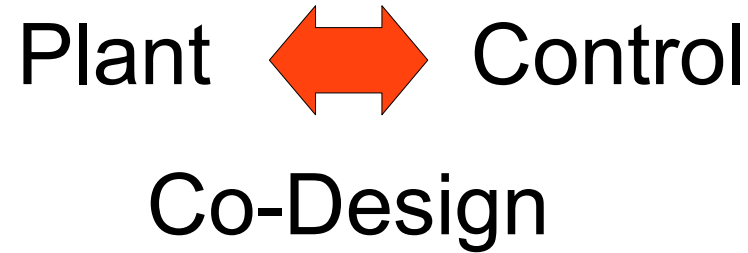
# Common activities in control system design

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- Open-loop analysis
  - steady-state operation
  - step responses
  - numerical linearization
- Closed-loop analysis
  - evaluation of different control strategies
  - verification of control system performance
  - empirical tuning of parameters
  - study of operating scenarios
- Identification of uncertain parameters
  - ad-hoc experiments (e.g. friction in motion control applications)
  - optimization-based fitting of transients

# The ideal setting



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Early design stages

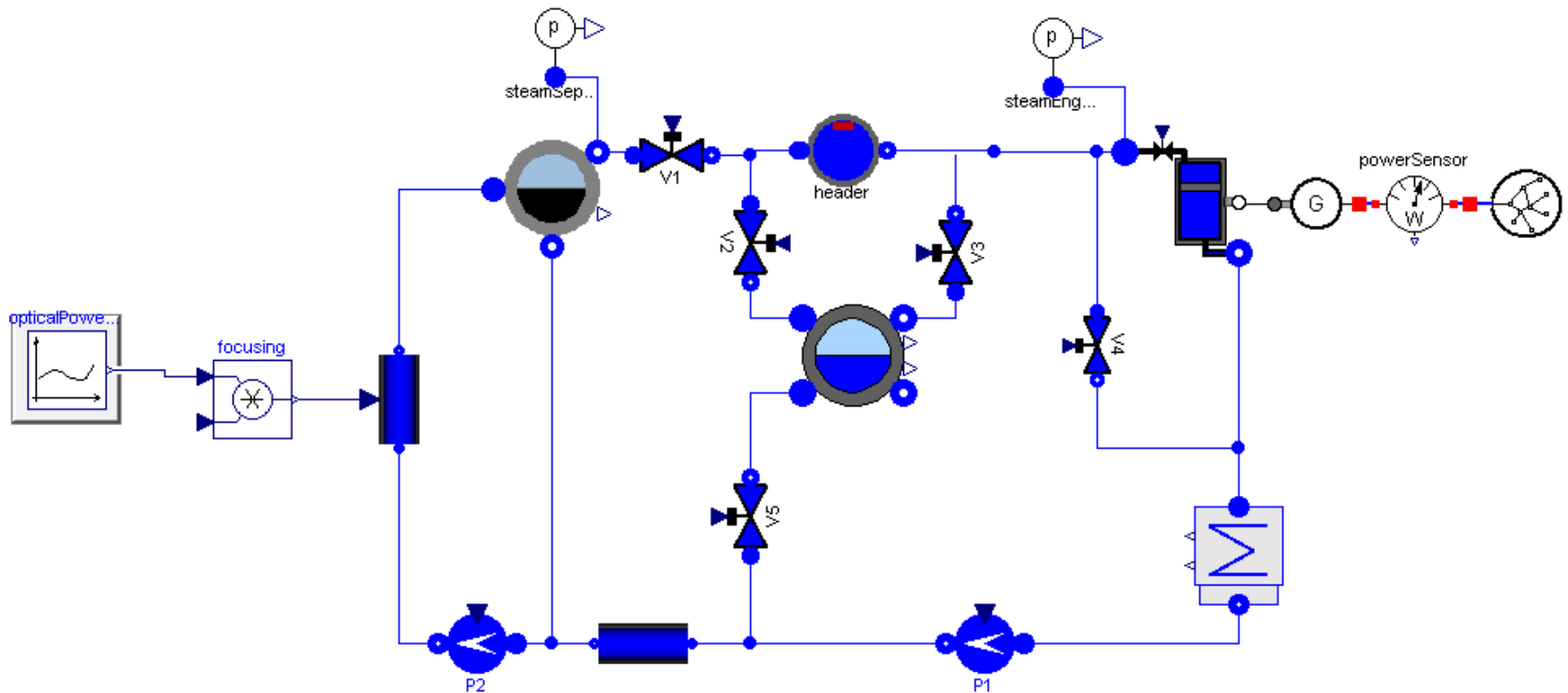
  
Detailed design & engineering

  
Commissioning

  
Operation  Revamping

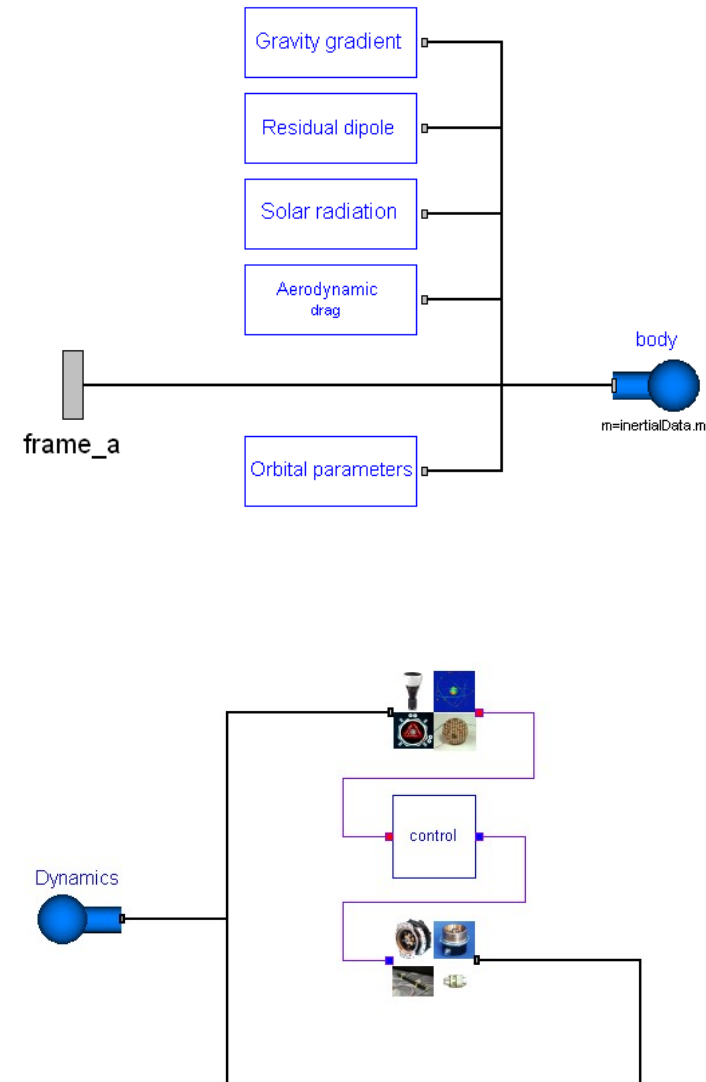
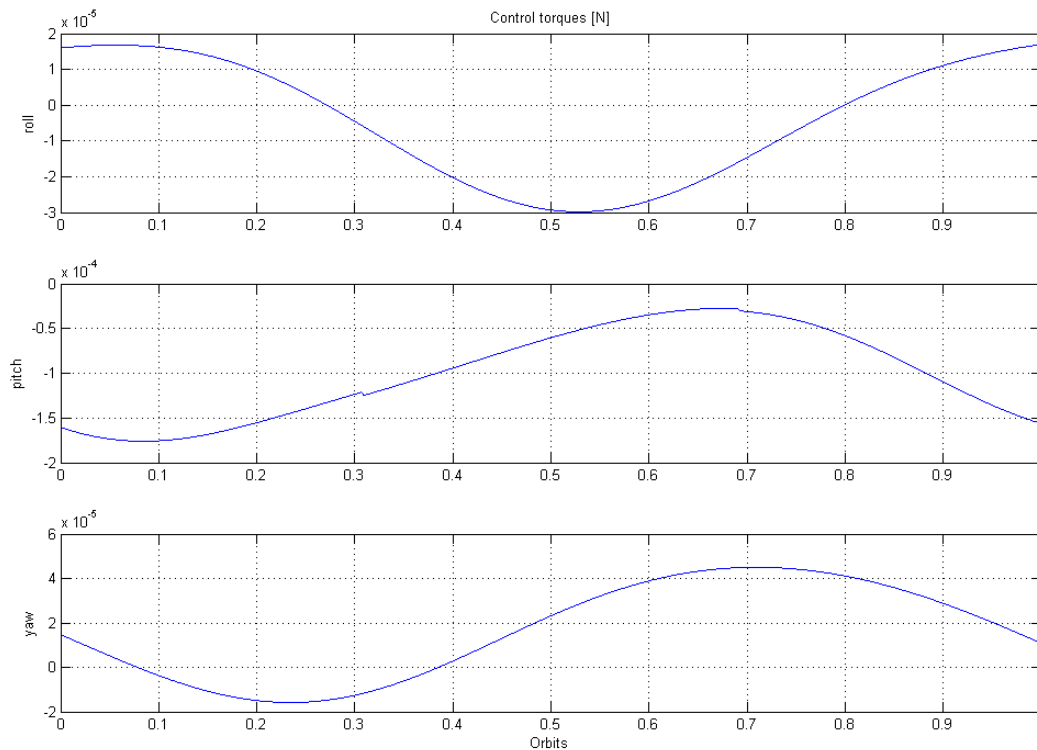
# Early design stages

- Few details available
- Evaluation of alternatives
- Closed-loop testing
  
- Example: solar power plant



# Early design stages – cont'd

- Model inversion for actuator sizing
- Example: satellite attitude control



# Detailed design

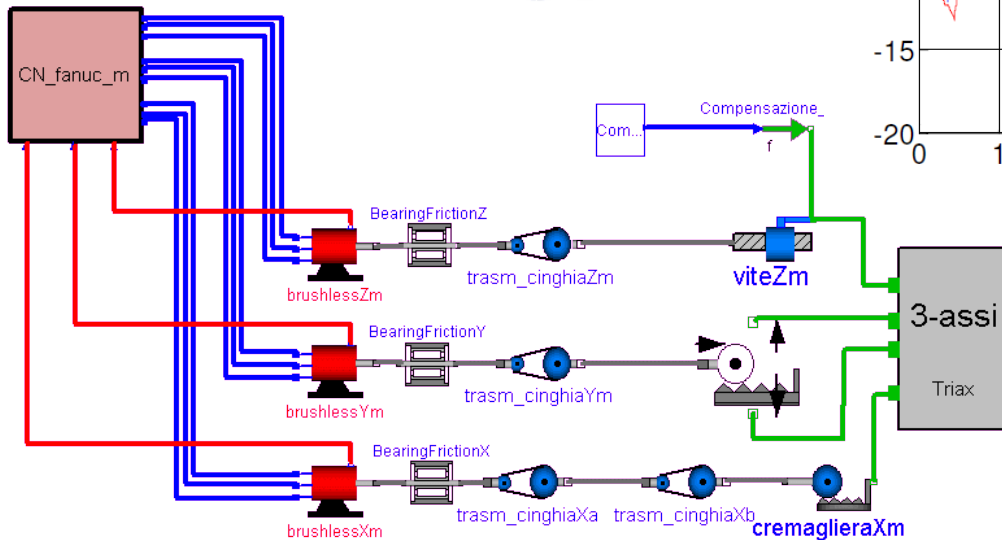
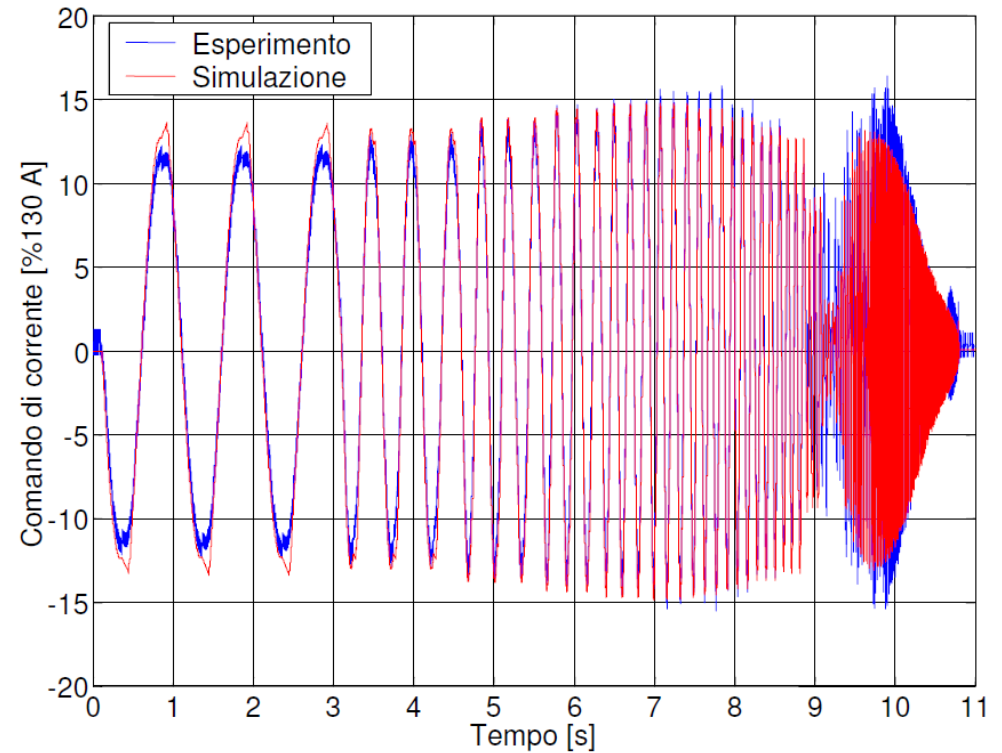
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- Refinement of sensors and actuators
  - satellite attitude control
  - pump/valves in thermo-fluid systems
  
- Refinement of plant model
  - more accurate physical model
  - second-order physical phenomena
  
- Refinement of control system model
  - digital control algorithms
  - start-up / shutdown / trip handling



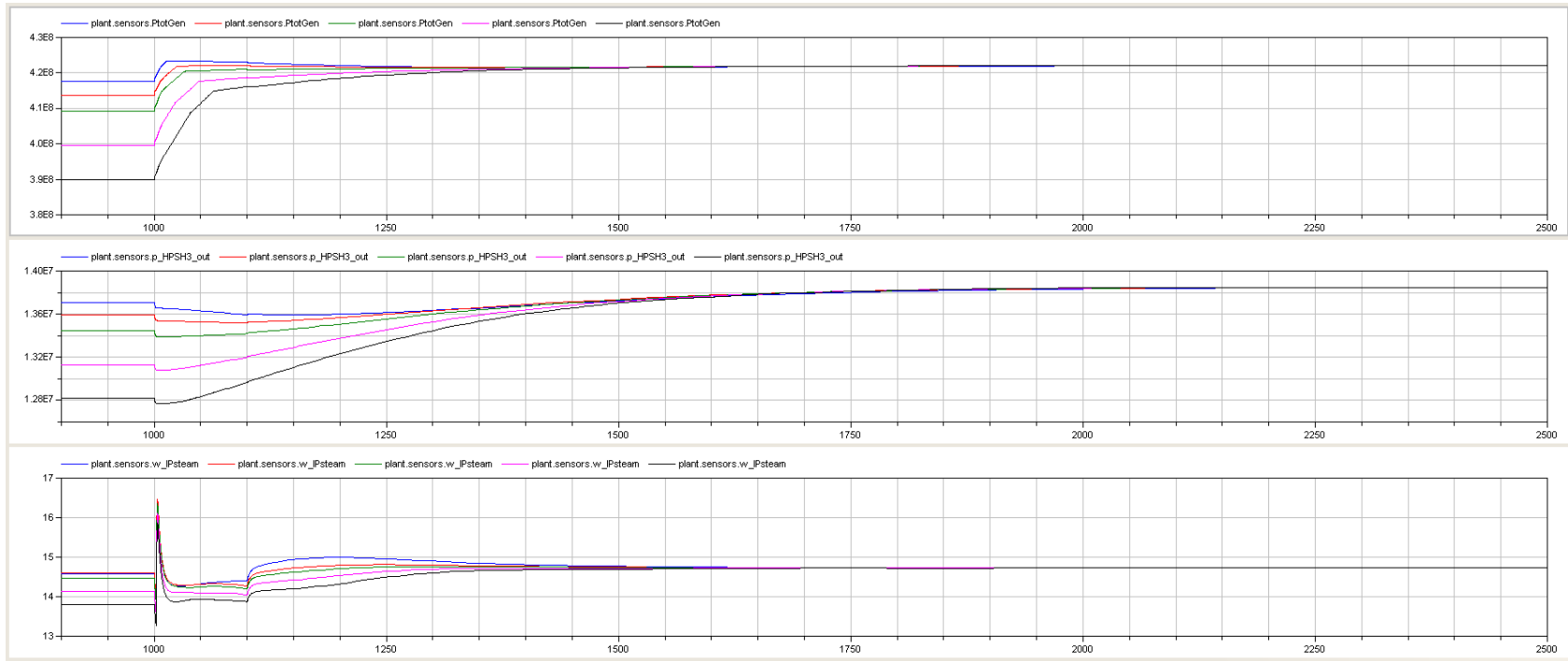
# Detailed design – cont'd

- Evaluation of critical plant dynamics
- Example: machining tool



# Commissioning

- Anticipating problems that might arise on-site during commissioning
- Reducing number of tests for CS acceptance
- Help understanding results of tests
- Example: power/frequency control in a 400 MW power plant



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How did all of this evolve?

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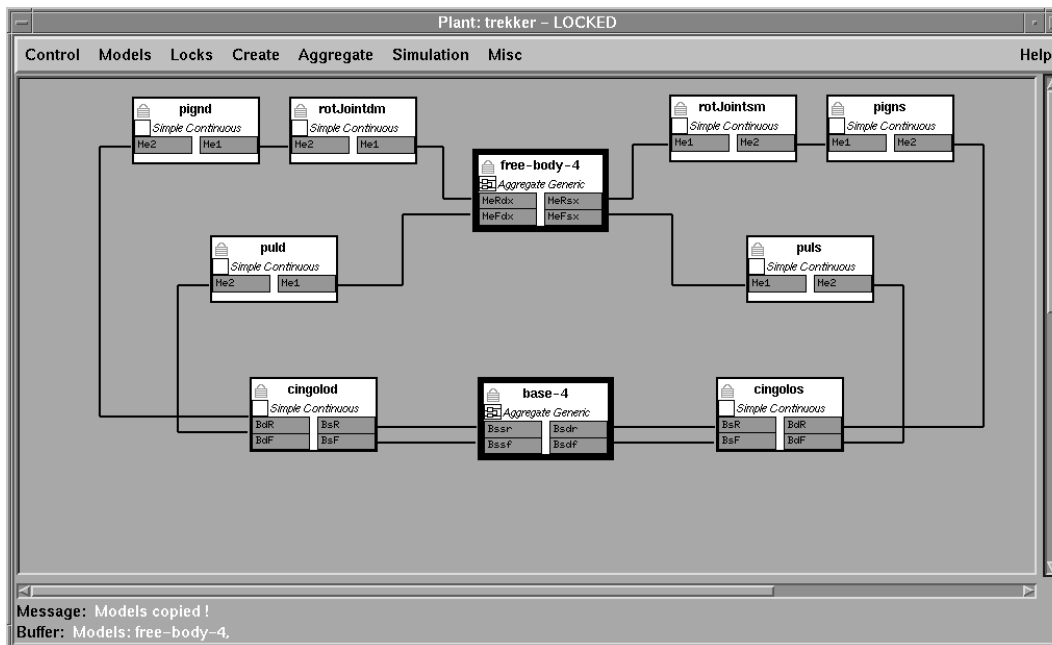
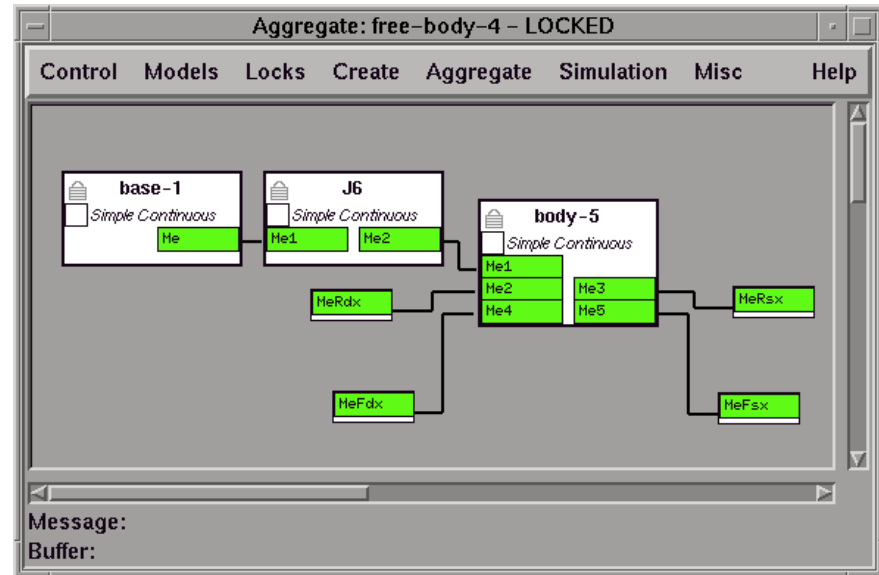
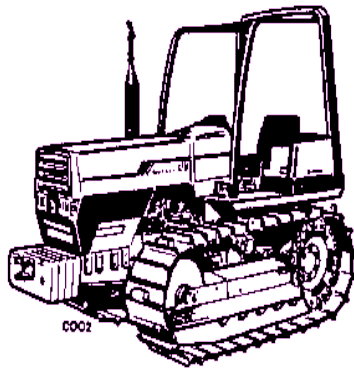
The Past  
*or*  
The Heroic '90s

# MOSES

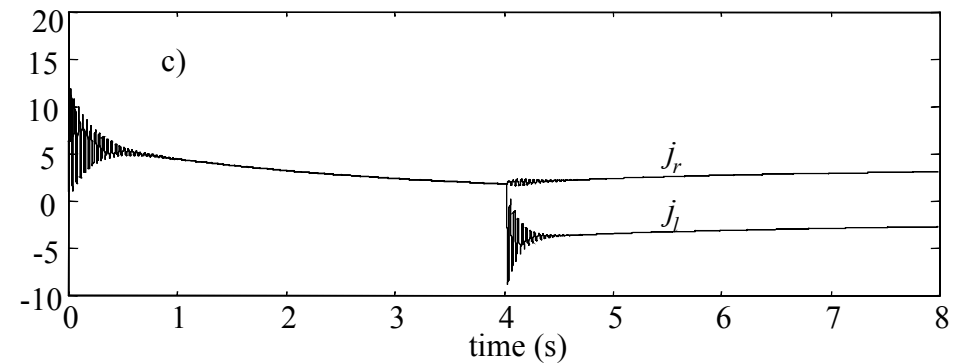
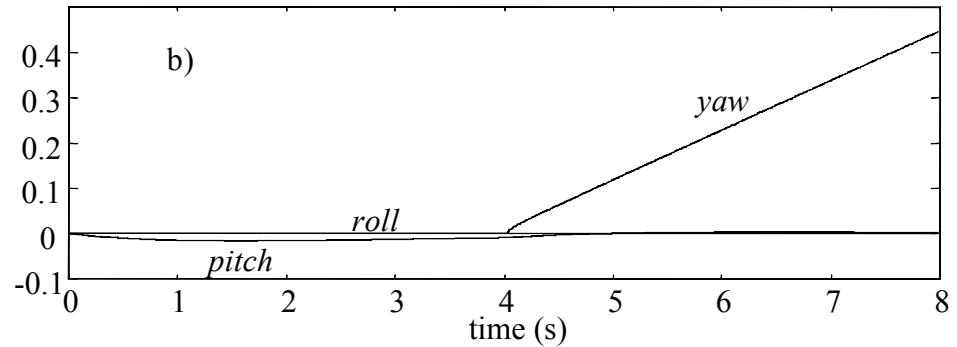
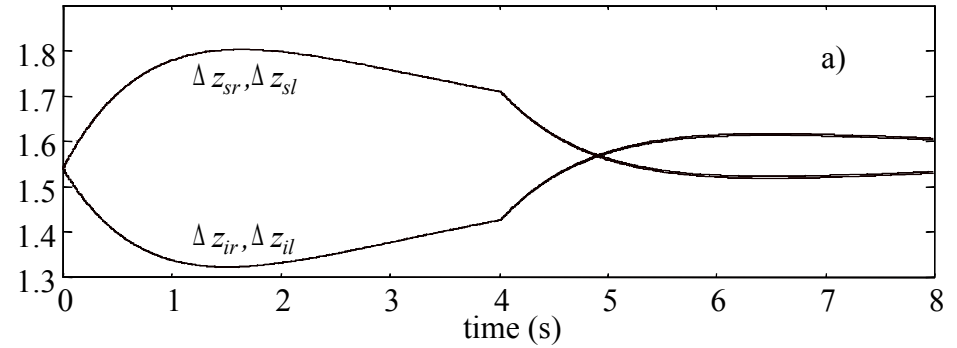
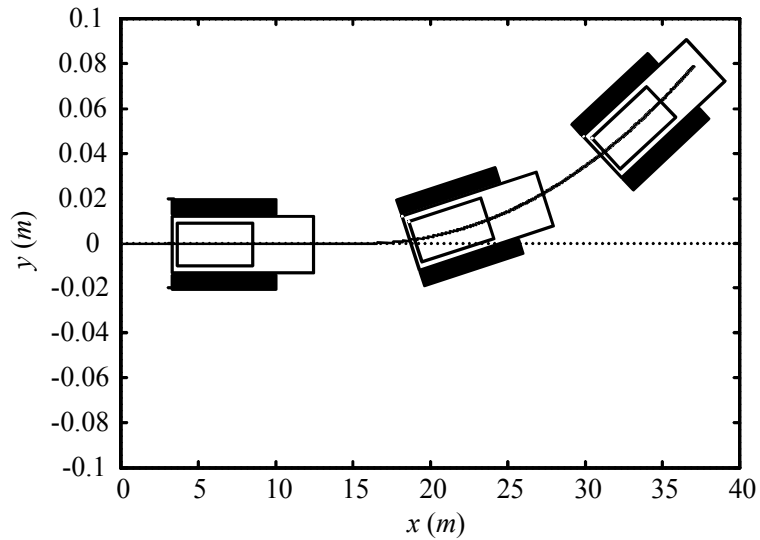
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- O-O Modelling tool developed @ Politecnico di Milano 1993-1998
  - effort led by prof. Claudio Maffezzoni
  - Roberto Girelli's PhD thesis
  - contributions by Emanuele Carpanzano and others
  
- Features
  - Equation-based, O-O models in an O-O database
  - Hierarchical composition
  - Multibody mechanical systems
  - Index reduction and automatic differentiation
  - Tearing
  - DASSL as ODE integrator

# Modelling of an agricultural tracked vehicle



# Modelling of an agricultural tracked vehicle – cont'd



# The heroic early '90

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- Equation-based, Object-Oriented modelling paradigm emerges
- Early tool implementations
- Prototype tools developed mostly in universities
- Proof-of-concept
- Heroic efforts in order to support real-life engineering projects



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# The Present

## 2000-2010

# A well-established paradigm

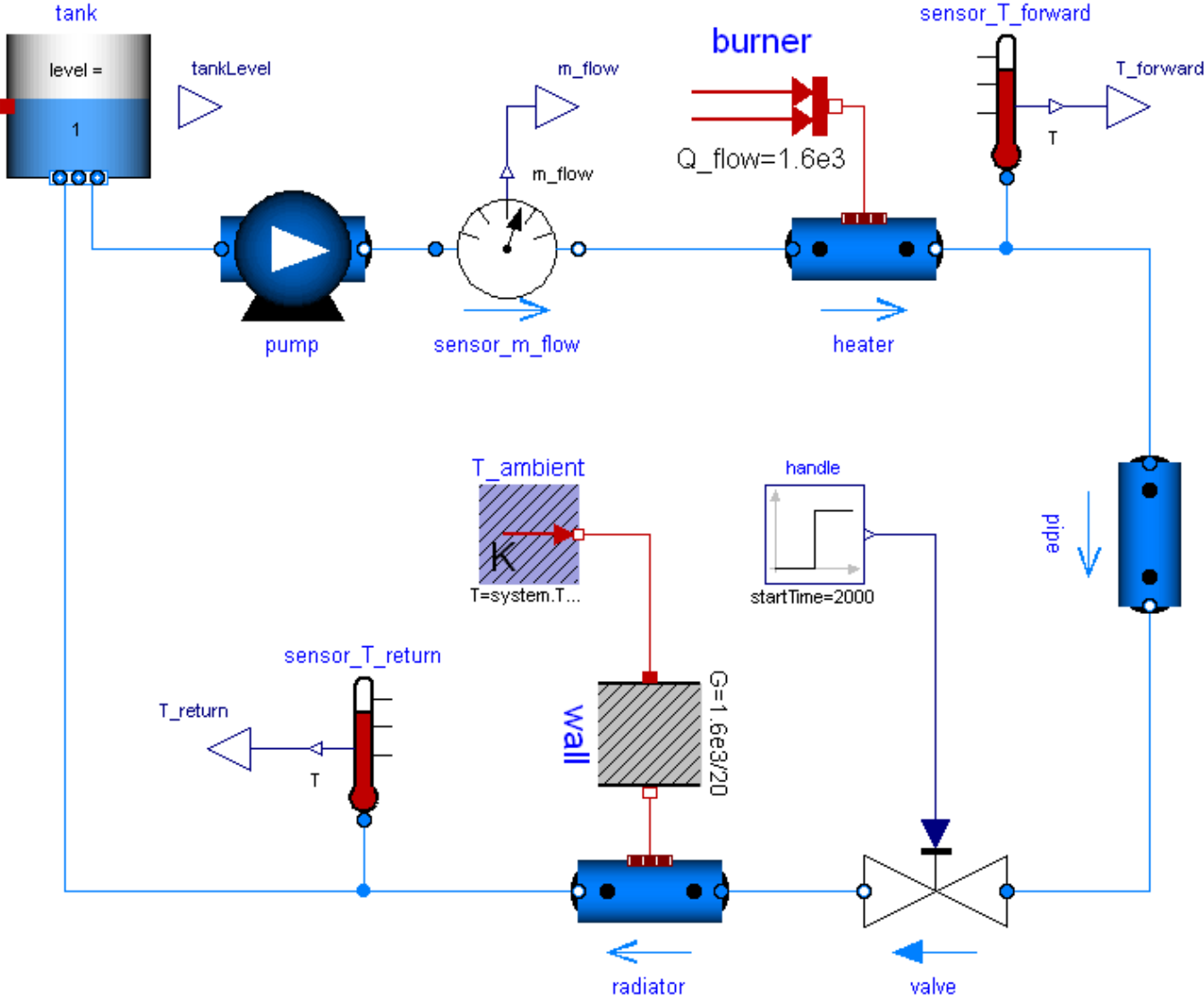
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- Modelica language evolves and into gets mainstream
- Increasing number of simulation tools available
- Used for real-life system engineering (and control engineering)
- Success stories
  - Automotive
  - Power plants
  - Robotics
  - Mechatronic systems
  - Aerospace
  - ...
- Reusable libraries
- European Projects
  - EuroSysLib
  - ModProd
  - Modelisar
  - ...
- Link with Systems Engineering Community

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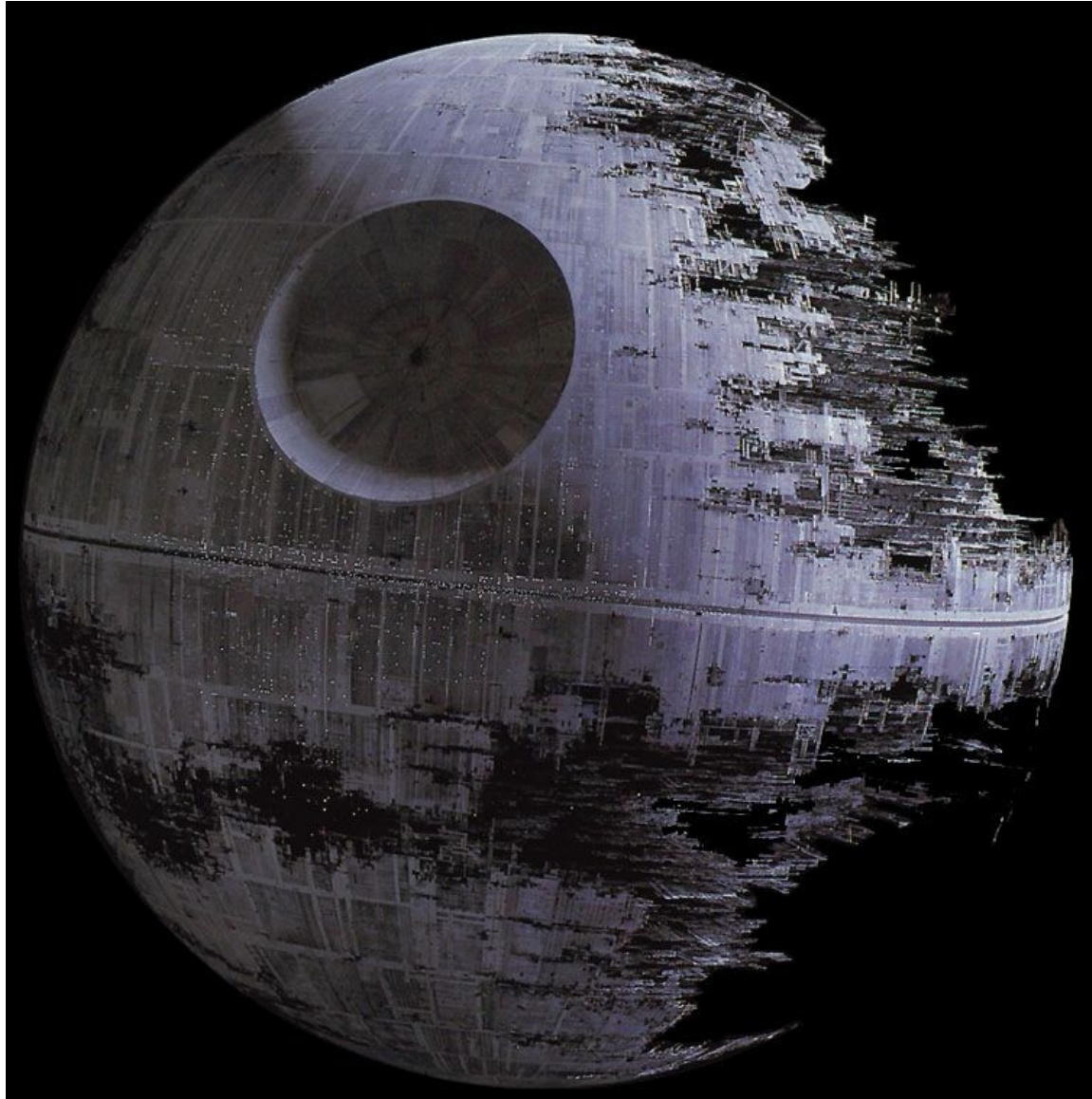
but...

# A (not so nice) anecdote



# The dark side of O-O modelling

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Description of model behaviour

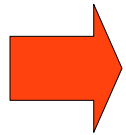
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*Description of initial state*

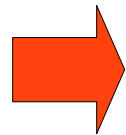
# Initial state descriptions

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- Problem #1: the initialization problem is a *system-level* problem
  - issues with component-wise initial equation setting
  - singular configurations (e.g. closed fluid systems)
- Problem #2: the initial equations might be difficult to solve
  - nonlinear algebraic equations require initial guesses
  - steady-state initialization → large systems of equations
- Problem #3: given initial state values sometimes unsuitable
  - fluid and thermofluid systems: unphysical transient outside model validity range
  - “rest” state might be problematic (singular problem)
  - control studies often requires equilibrium as initial state



How to specify initial conditions conveniently?



How to solve the initialization problem reliably?

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The Future  
*or*  
2011 and beyond...



# Reliable automatic initialization

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- Getting a meaningful initial state is a key ingredient in dynamic modelling
- Shouldn't require a PhD in simulation methods
- Should be easy for the average engineer
- Should be easy to specify unambiguously
  
- Robust methods for initialization problems (no human intervention)
- Meaningful diagnostic feedback for engineers and domain experts
  
- Embed domain-specific knowledge into model (and meta-model) libraries

# Homotopy-based initialization

- Define a simplified problem which is easier to solve

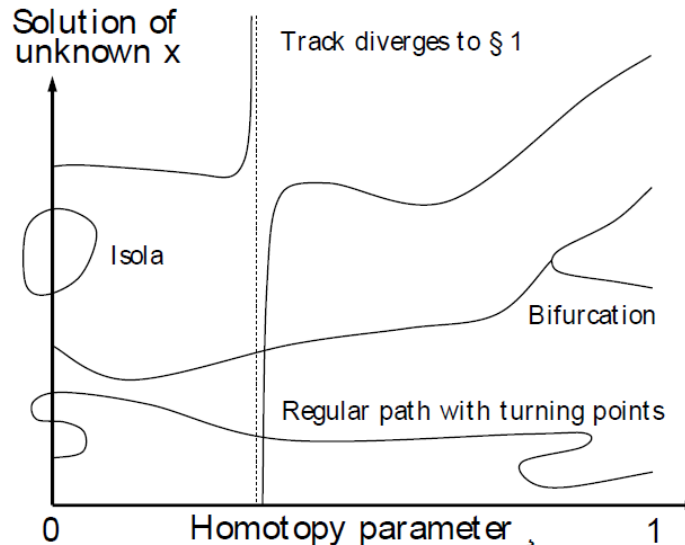
$$F_s(x) = 0$$

- Continuously transform into the actual problem

$$(1 - \lambda) F_s(x) + \lambda F_a(x) = 0$$

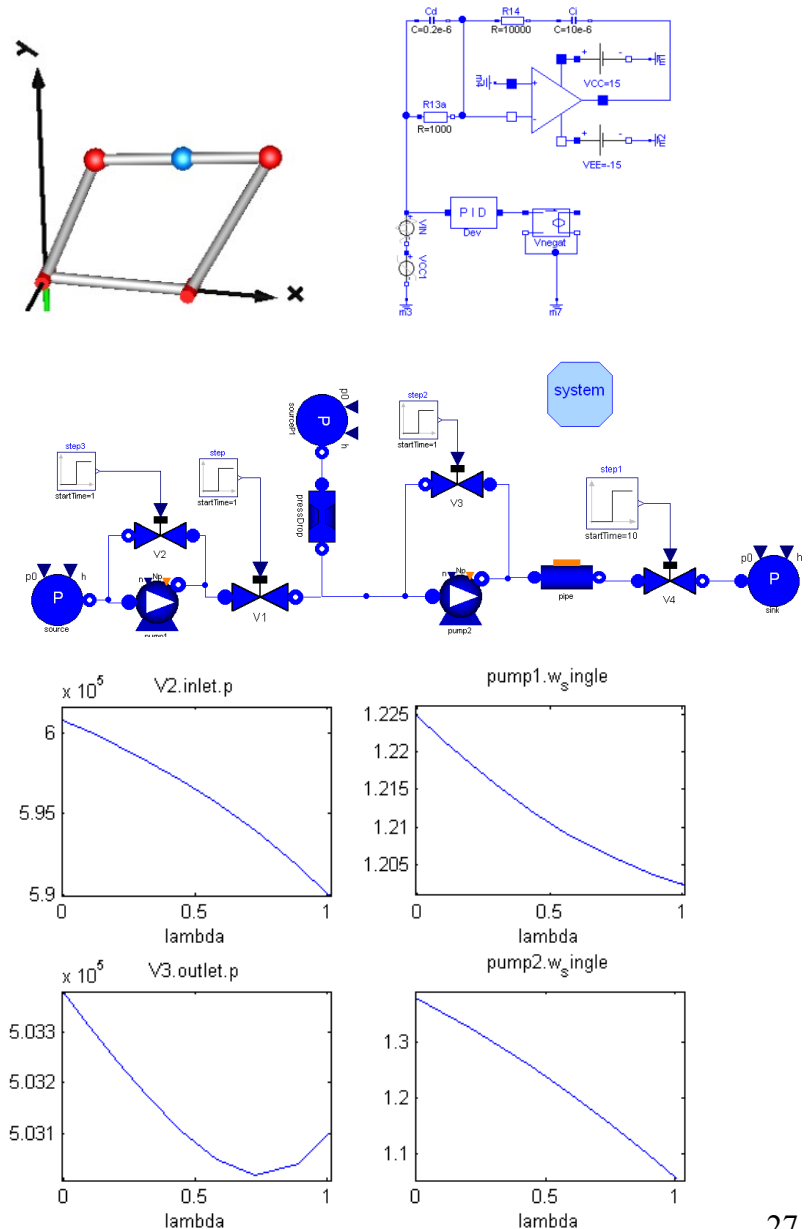
- New Modelica operator `homotopy(actual, simplified)`

- Beware of singularities!



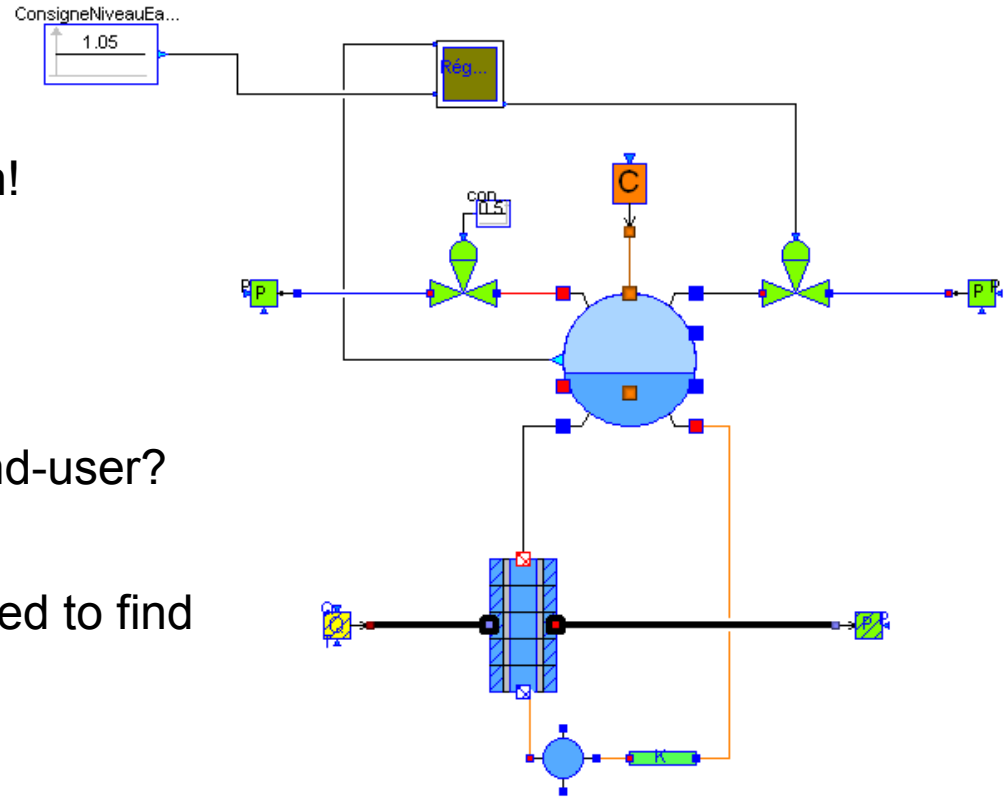
# Homotopy-based initialization – First results

- Multibody systems with multiple configurations
- Analog electronic circuits
- Hydraulic networks
- Calibration of air-conditioning systems
- Large power plants
- Two papers at the next Modelica Conference
- One possible way to embed expert knowledge to help the end user



# Improved support for troubleshooting

- The strange case of the steam generator
- “Wrong” parameters  
→ no steady-state solution!
- Dynamic analysis
- Meaningful hints for the end-user?
- Substantial research needed to find general solutions!



# Improved support for troubleshooting – cont'd

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- Troubleshooting singular initialization problems
- The case of steady-state initialization of closed-loop circuits

$$\frac{dM_1}{dt} = w_1 - w_2$$

$$\frac{dM_2}{dt} = w_2 - w_1$$

$$\frac{dM_1}{dt} = 0$$

$$\frac{dM_2}{dt} = 0$$

- How to give meaningful feedback to end-users in this case?

# Off-line and on-line optimal control

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$$\min_{x,u,z,p} \int_0^T l(t,x(t),\dot{x}(t),z(t),u(t),p) dt \\ + E(T,x(T),z(T),p)$$

subject to

$$f(t,x(t),\dot{x}(t),z(t),u(t),p) = 0 \quad t \in [0, T]$$

$$h(t,x(t),\dot{x}(t),z(t),u(t),p) \leq 0 \quad t \in [0, T]$$

$$x(0) = x_0$$

$$u_{\min} \leq u(t) \leq u_{\max} \quad t \in [0, T]$$

$$p_{\min} \leq p \leq p_{\max}$$

- System model described in Modelica
- Additional settings described in Optimica (small extension of Modelica)
- Jmodelica tool: optimization back-ends
  - IPOPT (direct collocation method)
  - ACADO (multiple-shooting)
- Off-line optimization
- On-line optimization (MPC)

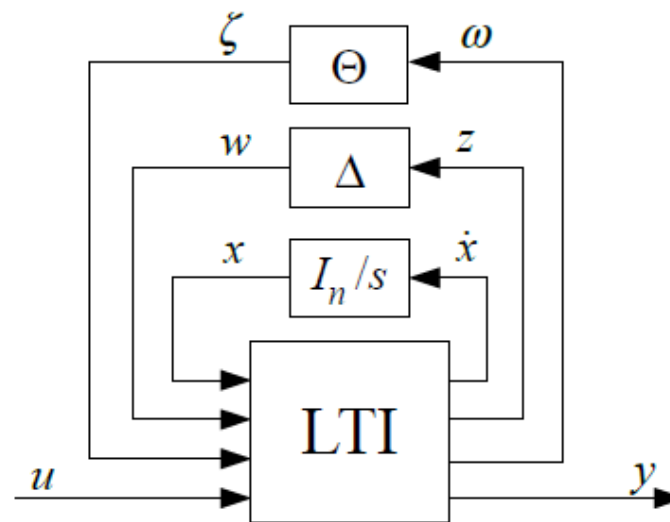
# Transformation of models into control-oriented formalism

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- Beyond simulation: model transformation
- Control design methods require models with special structure as input
  - linear state-space
  - nonlinear state-space
  - piecewise linear or affine
  - linear-parameter-varying (LPV)
  - linear fractional representation (LFR)
- Modelica front-end helps closing the theory-practice gap

# Modelica → LFR

- Prototype implementation of Modelica → LFR transformation
  - developed @ Politecnico
  - uses OMC+ Maxima + LFR toolbox (ONERA/DLR)



- Application
  - Robust control
  - Gain-scheduling control
  - Gray-box identification

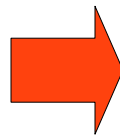


# Nonlinear Model Order Reduction

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- Simulation oriented models usually too complex for direct use in model-based control system
- Model reduction techniques required
- Define reference scenario(s)
- Define maximum acceptable error
- Rank terms in equations according to sensitivity on output error
- Eliminate / approximate them progressively
- Used in behavioural modelling of digital IC's (Analog Insydes)
- Prototype tool Univ. Duisburg (→ fast real-time performance)

Accurate / general  
simulation models

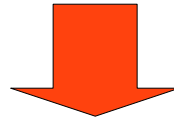


Fast / smooth / low-order  
control-oriented models

# Conclusions

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- OOM is a blessing for the control engineer (esp. w.r.t. block-oriented)
- Initialization is currently Achille's heel
- Models mainly used for simulation\



- More reliable, automatic, and user-friendly specification and solution of initialization problems
- More end-user relevant feedback in case of trouble
- Model Order Reduction
- Model transformation into control-oriented formalism
- Direct support for optimal control and MPC

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Thank you for you kind attention!