

# Pure Modelica Unit Testing: From Mathematical Algorithms to Physical Modeling

OpenModelica Annual Workshop 2019

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# Outline

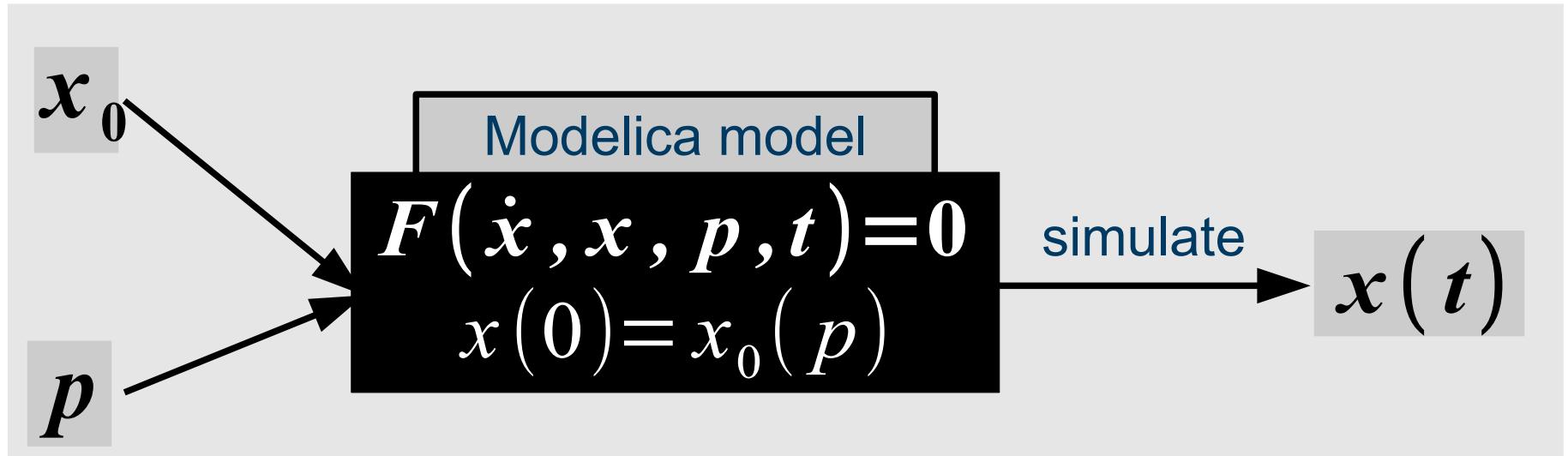
- First testing experiences
  - Mathematical algorithms in Modelica
- Unit testing in Modelica
  - existing technologies
- A bit more “formal” Unit testing
  - Upgrading to Physical Modeling

# Motivation

Wiechert, W., Noack, S., and Elsheikh, A. (2010).  
Modeling languages for biochemical network  
simulation: Reaction vs equation based approaches.  
Advances in Biochemical Engineering / Biotechnology

“Simulation tools not only perform numerical  
solutions based on the system equations but  
also assist the modeler in systems analysis.  
Doubtlessly the most important systems analysis  
tool is Sensitivity Analysis ...

# SA of Modelica Models

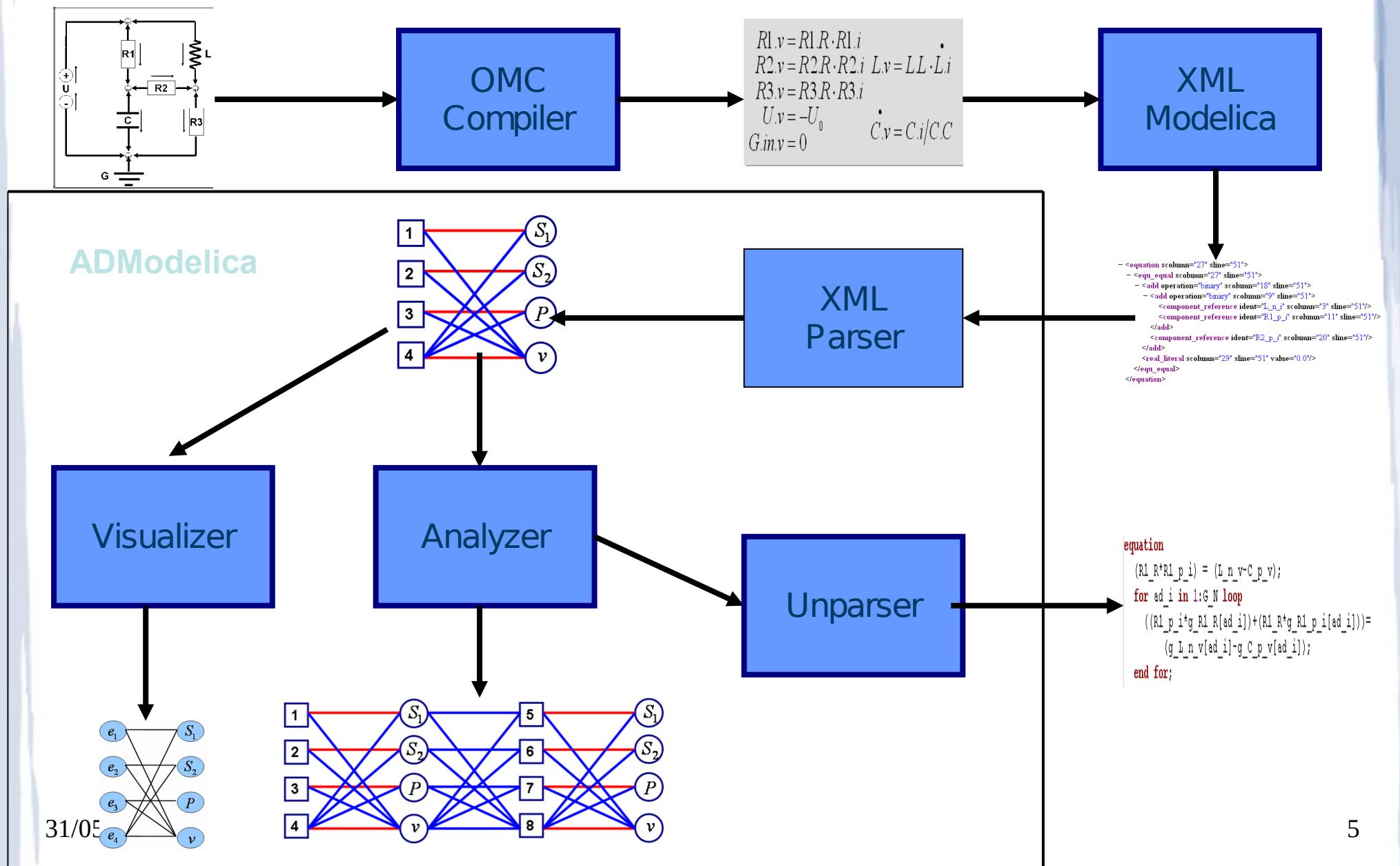


**Dynamic Parameter  
Sensitivities (DPS)**

$$\frac{\partial x}{\partial p}(t)$$

$$\frac{\partial x}{\partial x_0}(t)$$

# ADModelica (2007)



# Sample of generated code

(I/II)

- Declaration part

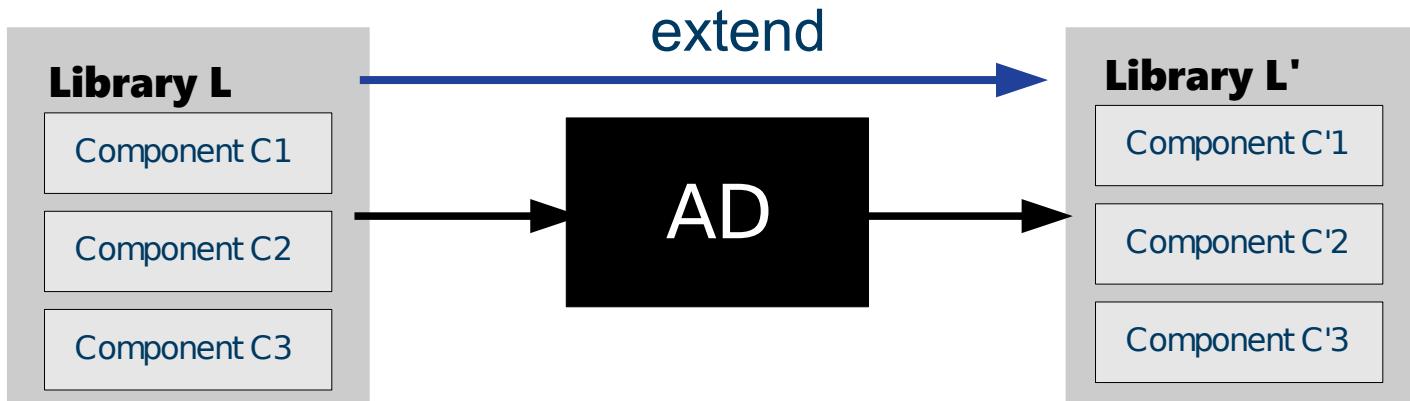
```
model ADSimpleReaction
  Real S(start=1);
  Real P(start=0);
  Real v;
  Real[3] g_S, g_P, g_v;
  parameter Real vmax=1;
  constant Real[3] g_vmax={1,0,0};
  parameter Real k=1;
  constant Real[3] g_k={0,1,0};
  parameter Real lk=1;
  constant Real[3] g_lk={0,0,1};
protected
  Real loc01,loc02,loc03,loc04,loc05;
  Real g_loc01,g_loc02,g_loc03,g_loc04,g_loc05;
```

# Sample of generated code (II/II)

- Equation part

```
equation
  der(S)=-v;
  der(P)=v;
  //v = vmax * (S/(S+k)) * (Ik/(P+Ik));
algorithm
  loc01 := vmax*S;
  loc02 := S+k;
  loc03 := loc01/loc02;
  loc04 := P+Ik;
  loc05 := Ik/loc04;
  v     := loc03*loc05;
//Derivatives:
equation
  for i in 1:3 loop
    der(g_S[i])=-g_v[i];
    der(g_P[i])=g_v[i];
  end for;
algorithm
  for i in 1:3 loop
    g_loc01 := g_vmax[i]*S+vmax*g_S[i];
    g_loc02 := g_S[i]+g_k[i];
    g_loc03 := (g_loc01*loc02-loc01*g_loc02)/(loc02^2);
    g_loc04 := g_P[i]+g_Ik[i];
    g_loc05 := (g_Ik[i]*loc04-Ik*g_loc04)/(loc04^2);
    g_v[i]  := g_loc03*loc05+loc03*g_loc05;
  end for;
end ADSimpleReaction;
```

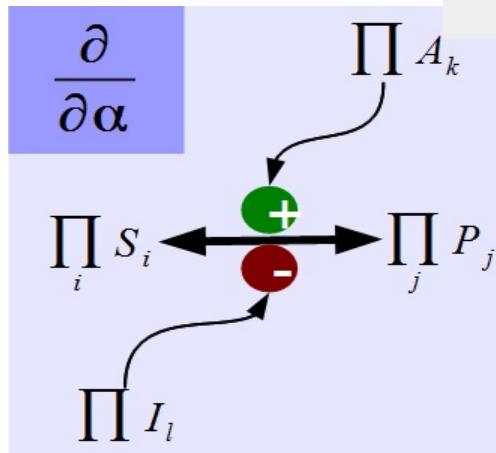
# Algorithmic Differentiation (AD) of Modelica libraries (2011)



# Algorithmic differentiation Modelica Libraries

## The ADGenKinetics Library

2011

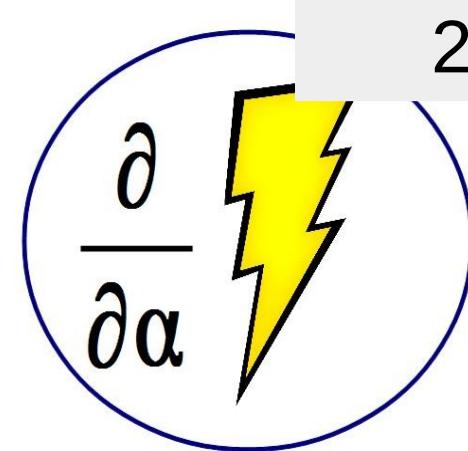


Algorithmically differentiated  
Modelica library for biochemical  
reaction networks

<https://github.com/modelica-3rdparty/ADGenKinetics>

## The ADMSL Library

2014



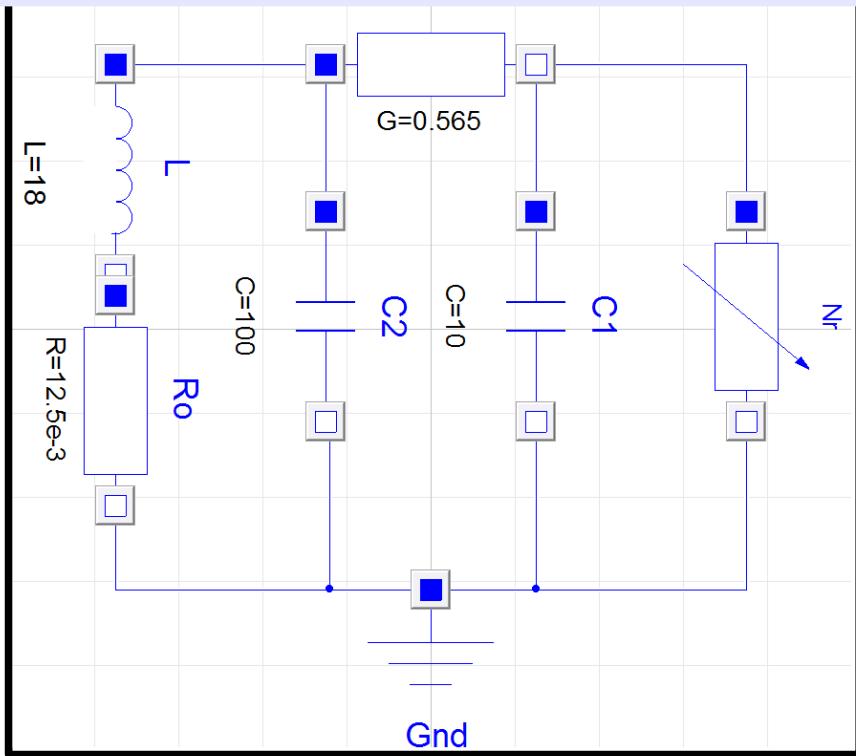
Serves as an example of  
algorithmically differentiated  
Modelica library

<https://github.com/AIT-CES-LAB/ADMSL>

# Chua Circuit

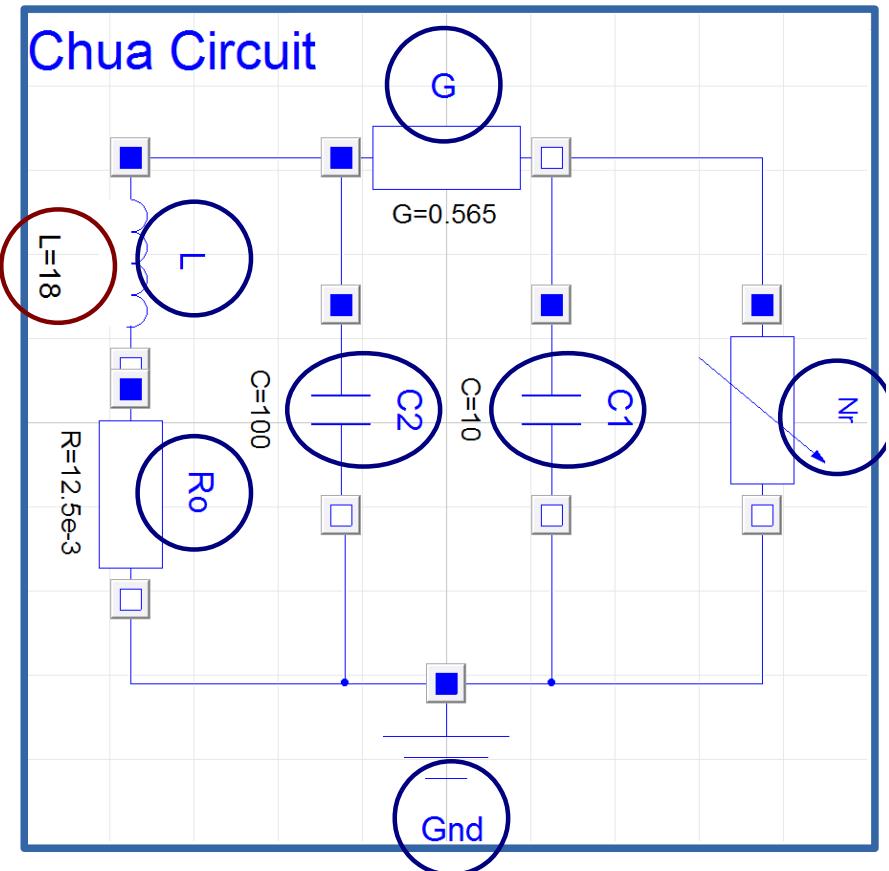
Standard Modelica model for an electrical circuit

`Modelica.Electrical.Analog.Basic.Examples.ChuaCircuit`



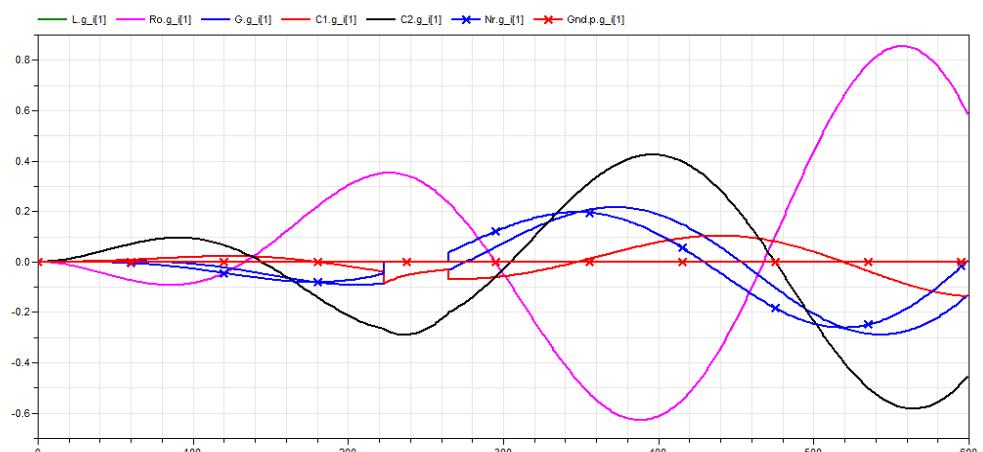
This example simulates  
the current and voltage  
at all components

# Chua Circuit importing ADMSL

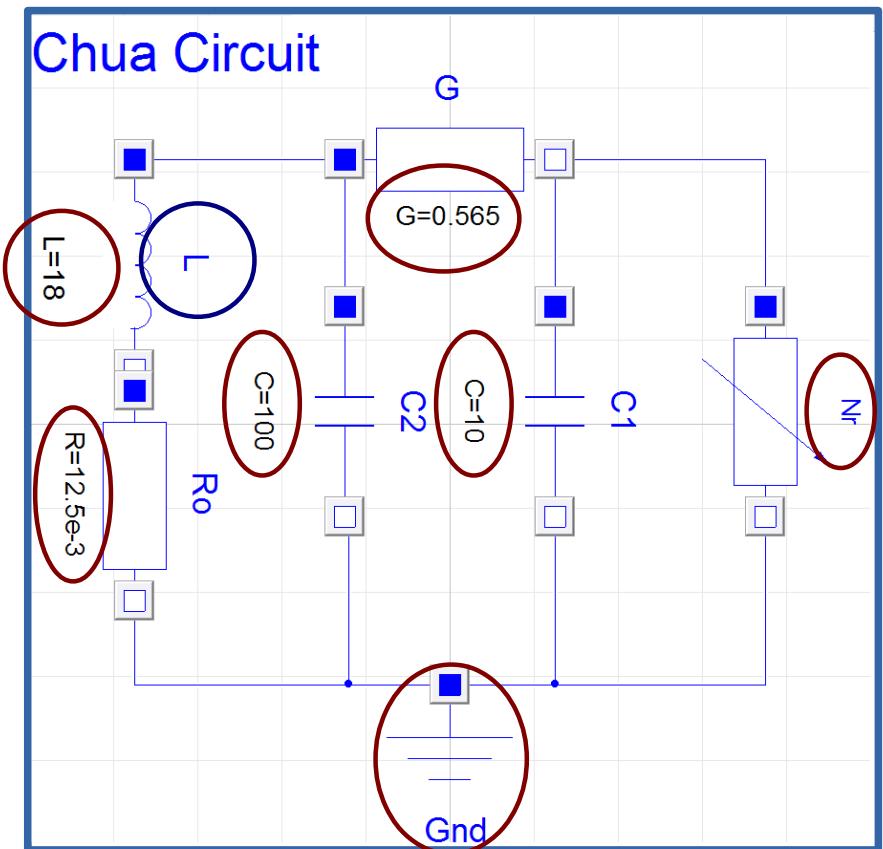


The sensitivities of the current w.r.t.  $L$

$$\frac{\partial X.i}{\partial L.L}$$

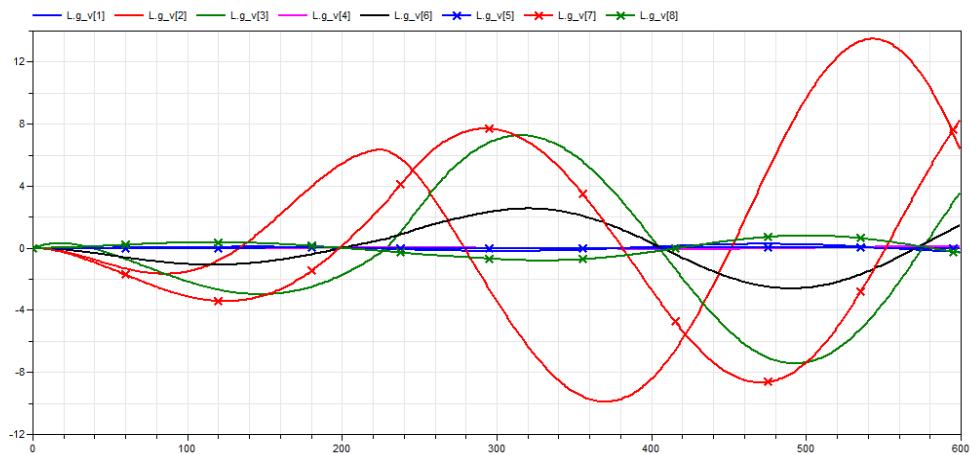


# Chua Circuit importing ADMSL



The sensitivities of the voltage at  $L$   
w.r.t. all parameters

$$\frac{\partial V_L}{\partial X.p}$$



# Applications of DPS

## 1) Modeling-Oriented

Control Coefficients, Local SA, Parameter Sweeping Studies,  
Model Simplification, ...

## 2) Statistical

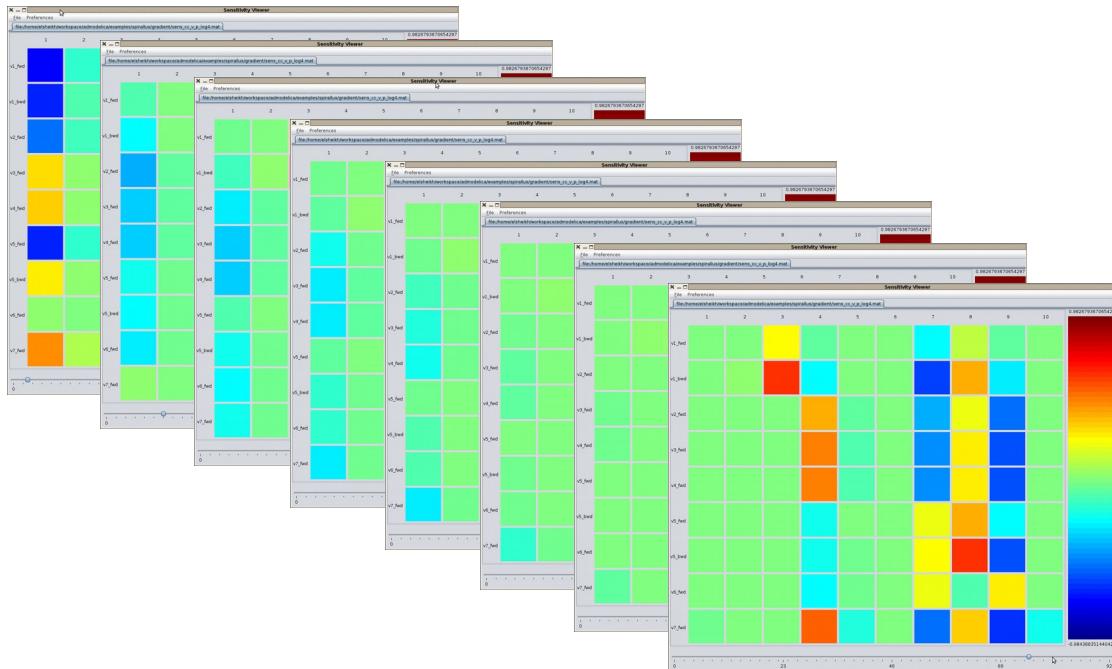
Regression Analysis, Global SA, Identifiability Analysis, ...

## 3) Optimization

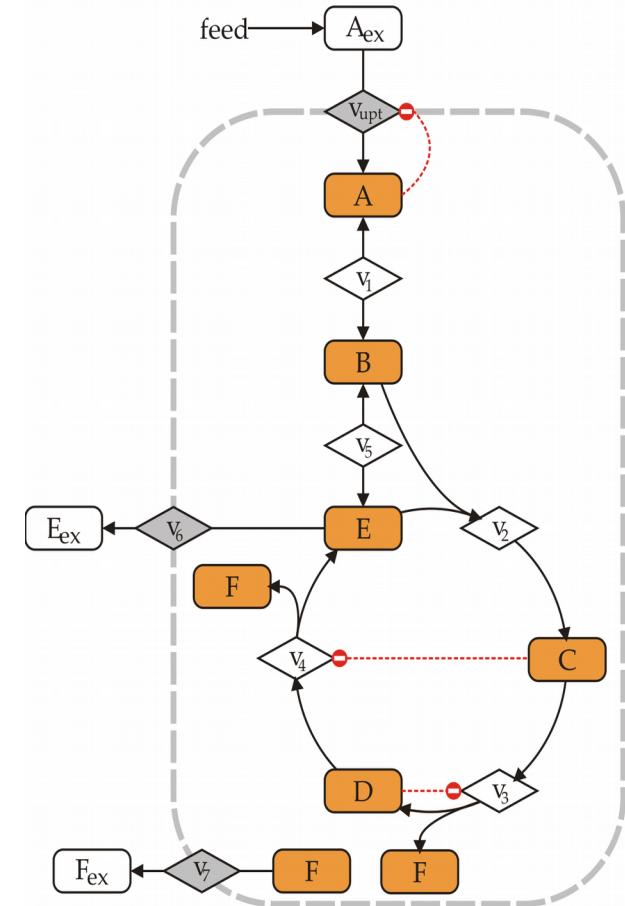
Cost-functions expressed in terms of DPS

# Scaled Parameter Sensitivities

$$CC_p^x = \frac{p}{x(t)} \frac{\partial x}{\partial p}(t)$$

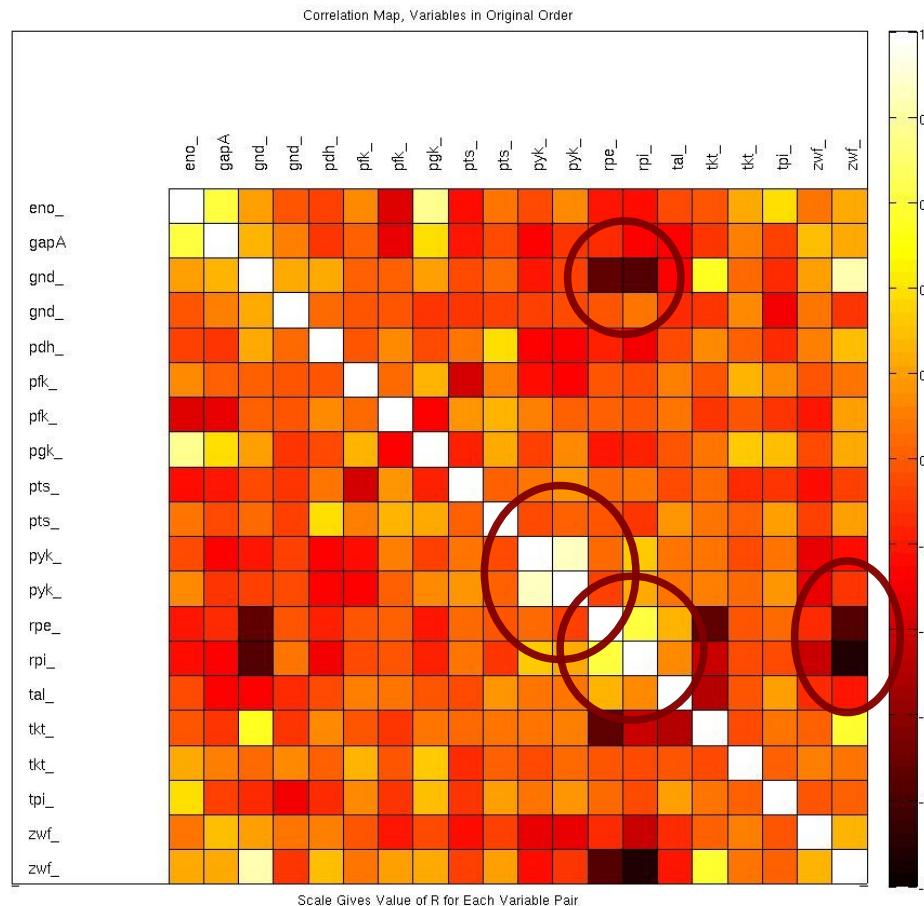


Several snapshots at different time points



# Correlation among parameters

## Correlation among parameters Based on Fischer Information Matrices



Strongly  
Correlated  
Parameters

# Testing AD

## Finite Difference Methods

$$\frac{\partial x}{\partial p_j}(t, p) = \frac{x(t, p + e_j \delta_j) - x(t, p)}{\delta_j} + O(\delta_j)$$

$$\delta_j = \epsilon p_j$$

## Adhoc Testing (2007-2014)

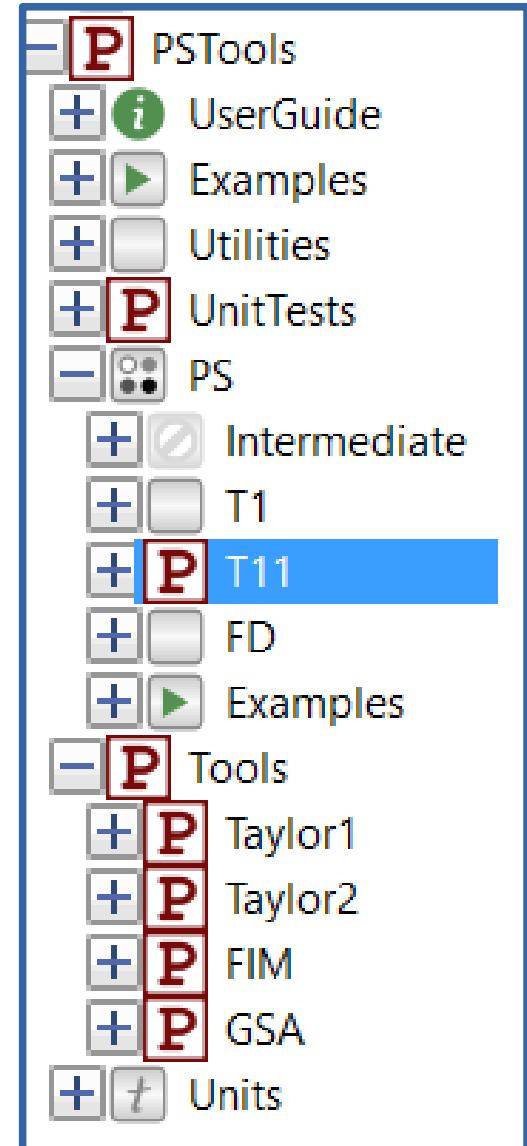
- 1) Evaluate DPS with FD  
externally with Matlab  
small models
- 2) Simulate AD models
- 3) Check if the curves behave similarly  
Sometimes compute Relative errors
- 4) Investigate cause of errors, if any

# Under Development (2019) Highly Experimental

## PSTools Library

- Promotes the usage of PS at Modelica level
- Serves as utility package for arbitrary Modelica libraries
- PS Package
  - Extensive set of examples for analytical derivatives
    - Including hybrid systems
  - Generic Models for advanced FD
  - Second-order DPS
- Tools Package
  - Taylor series approximation
  - Parameter Sweeping studies
  - Control Coefficients
  - ...

Unit Testing is must

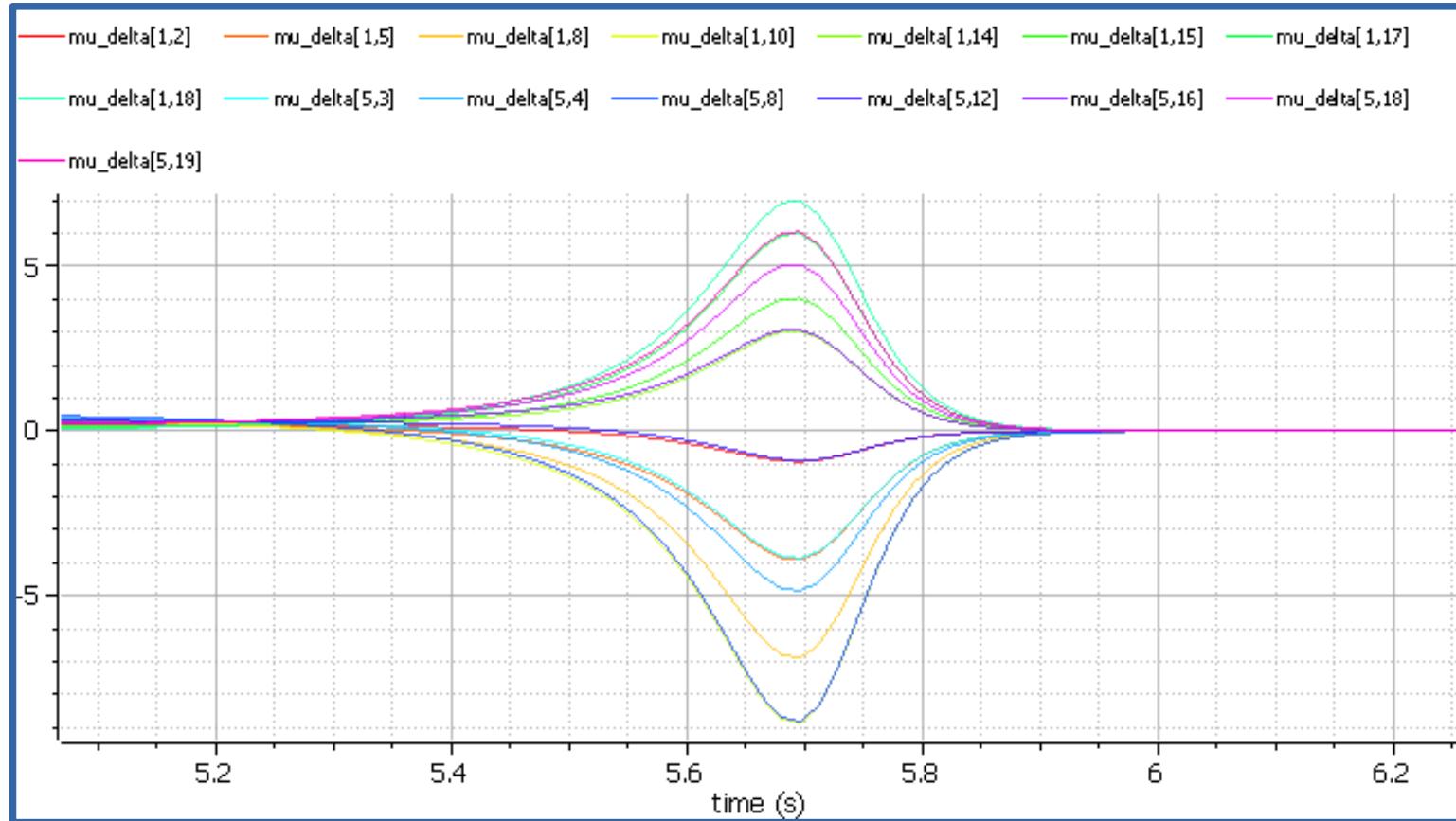


# FD with PSTools

```
model ParM
  extends Utilities.Parameterized(
    NP = 2,
    _P = {0.4, 0.5},
    PNAME = {"p1", "p2"},
    NX = 2,
    _X = {_M.x1, _M.x2},
    XNAME = {"x1", "x2"}
);
protected
  MyModel _M(
    p1 = _P[1],
    p2 = _P[2]);
end ParM;
```

```
model FDParM
  PSTools.PS.FD.CD2
  PS(redeclare replaceable
      Model ParModel = ParM);
end FDParM;
```

# Parameter Sweeping Studies



Jan Peter Axelsson & Atiyah Elsheikh  
Example of Sensitivity Analysis with the Bioprocess Library  
Modprod 2019

# Unit Testing Technologies for Modelica

Marco Kessler, Testing Tutorial  
Dassault Systems, Modelica 2017 Prague ([Link](#))

- CSV Compare – ESI ITI
- BuildingPy – LBNL
- PySimulator – DLR
- test.openmodelica.org
- XogenyTest – Xogeny
- Model Management – Dymola
- Testing tool kits (many Companies)
- Testing Library -- Dymola

# XogenyTest

- Pure Modelica
- Minimal
  - external scripting
  - log files
- Easy to use
- No dependencies

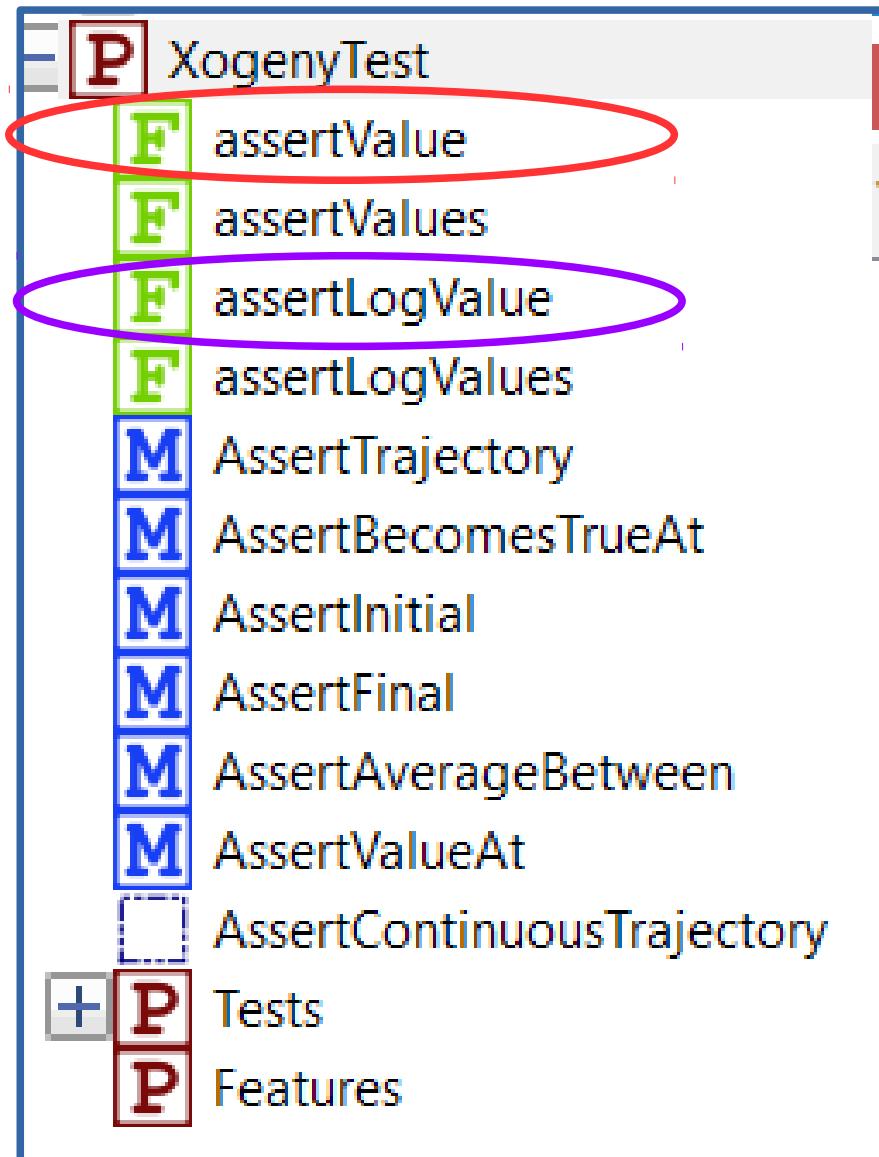
Not meant to be comprehensive but definitely an ideal getting start

Michael Tiller

<https://github.com/xogeny/XogenyTest>

Tiller, Michael M., and Burit Kittirungsi.  
"UnitTesting: A Library for Modelica Unit Testing"  
Modelica Conference Vienna, Austria, 2006

# XogenyTest



## Low level functions

asserting whether an expected value  $x$  lies within  $\epsilon$ -neighbourhood of a reference value  $r$  (i.e.  $N_\epsilon(r)$ )

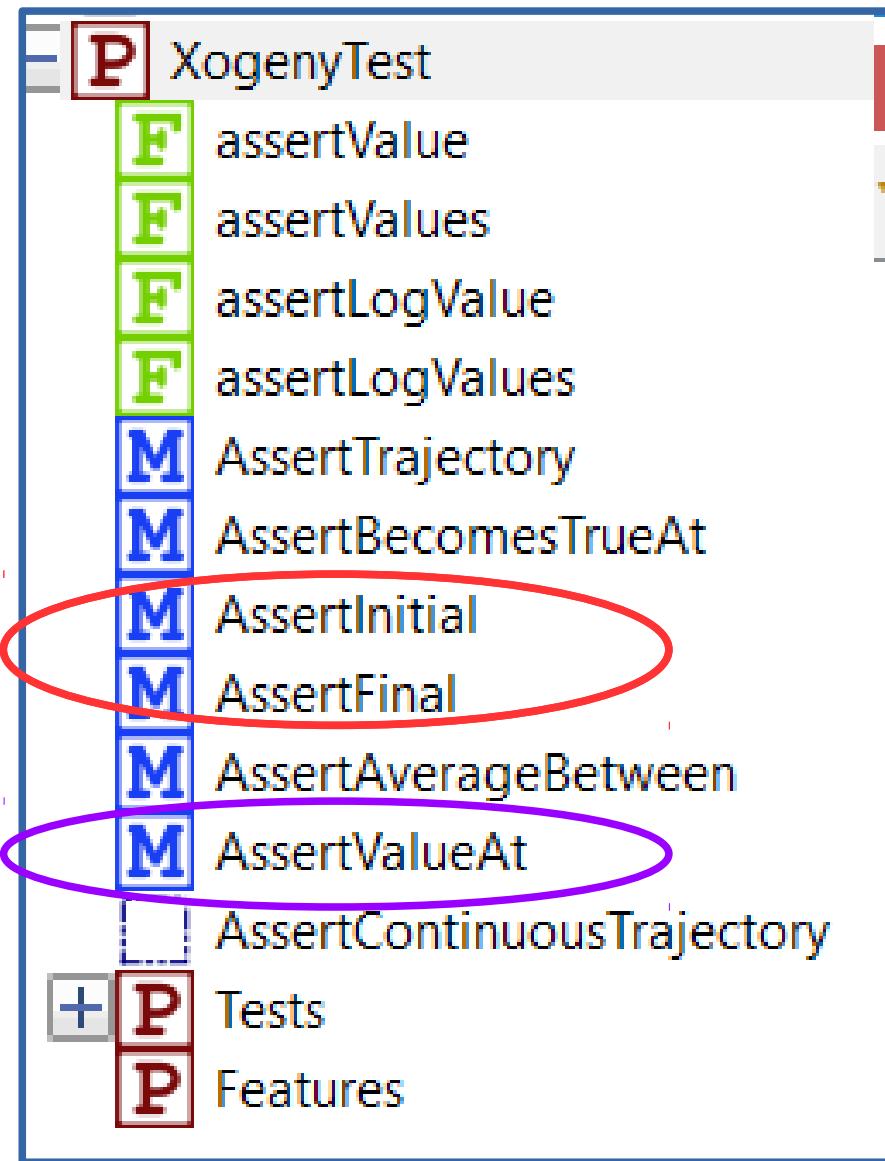
$$|x - r| < \epsilon$$

or

within the same order of magnitude

$$\log \frac{x}{r} < \epsilon$$

# XogenyTest



## Models

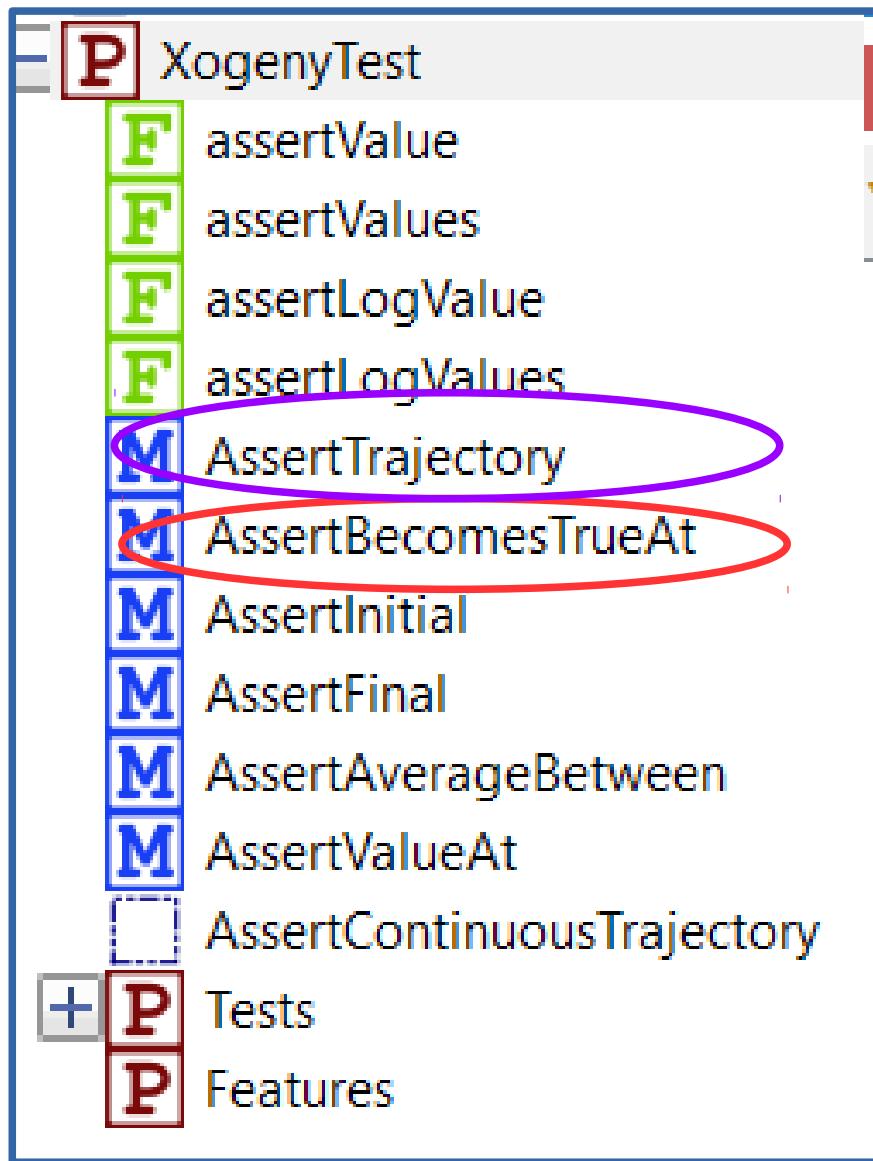
asserting an expected value  $x$  w.r.t. a reference value  $r$  at time  $T \in \{t_0, t_f\}$

$$|x(T) - r| < \epsilon$$

or at time  $t \in (t_0, t_f)$

$$|x(t) - r| < \epsilon$$

# XogenyTest



## Models

asserting an expected event  $e(t)$  occurs at time  $T$

$$e([T-\epsilon, T+\epsilon]) \rightarrow \text{True}$$

Asserting a trajectory  $x(t)$  at discrete time points  $\{t_1, t_2, \dots, t_N\}$  w.r.t. reference values  $r(t_i)$

$$|x(t_i) - r(t_i)| < \epsilon$$

# Examples (I/II)

```
model CheckSuccess
```

```
Real x = time^2;
```

```
AssertTrajectory check_x(  
    actual=x,  
    expected=[0,0; 1,1; 2,4; 3,9]);
```

```
Annotation(  
    TestCase(  
        action="simulate",  
        result="success"),  
    experiment(StopTime=4));
```

```
end CheckSuccess;
```

# Examples (II/II)

```
model CheckSuccess
```

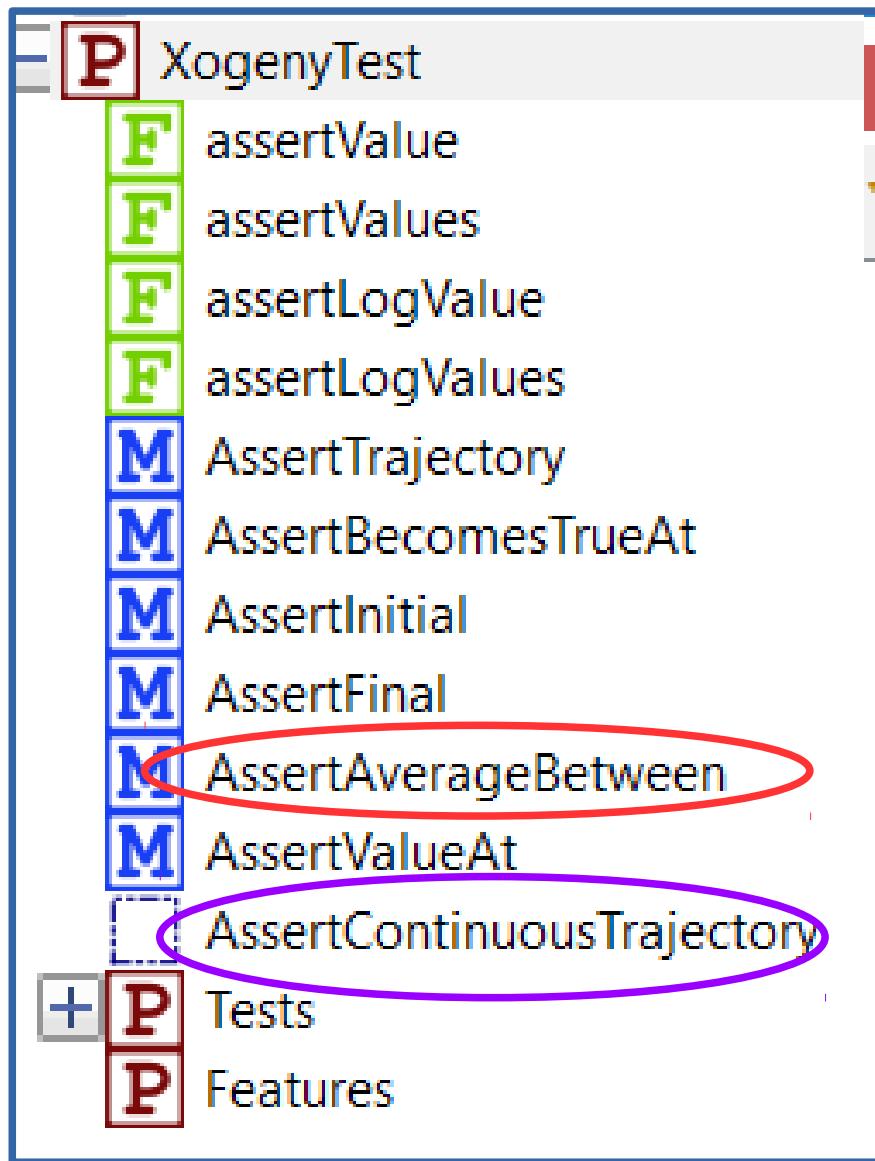
```
Real x = time;
```

```
AssertBecomesTrueAt  
  check_event(event=(x>2), at=2);
```

```
Annotation(  
  TestCase(  
    action="simulate",  
    result="success"),  
  experiment(StopTime=4));
```

```
end CheckSuccess;
```

# XogenyTest



## Models

Assert that a signal  $u(t)$  is of an average value  $a$  over  $[t_0, t_f]$

$$\frac{1}{t_f - t_0} \left| \int_{t_0}^{t_f} u(t) dt \right| - a < \epsilon$$

Asset that difference between trajectories  $x_1(t)$  and  $x_2(t)$  is less than accu. error  $A_{err}$

$$\int_{t_0}^{t_f} |x_1(t) - x_2(t)| dt < A_{err}$$

# Testing AD vs. FD

```
model TestT1BioProcess
import PSTools.Utilities.unitVector;

Utilities.Validate dmu_dKs(
    AccErr=1E-1,
    name="test T1.Processions dmu / dKs");

PSTools.PS.T1.BioProcess.Bioprocess PSAD(
    NG=1,
    g_Ks=unitVector(1, NG));

PSTools.PS.FD.BioProcess.BioProcess PSFD;
...
```

# Visual unit testing

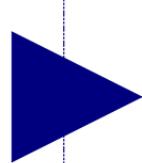
equation

```
dmu_dKs.T1 = PSAD.g_mu[1];  
dmu_dKs.T2 = PSFD.g_mu[1];
```

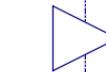
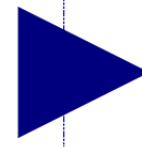
```
end TestT1BioProcess;
```

**Utilities.Validate**

T1

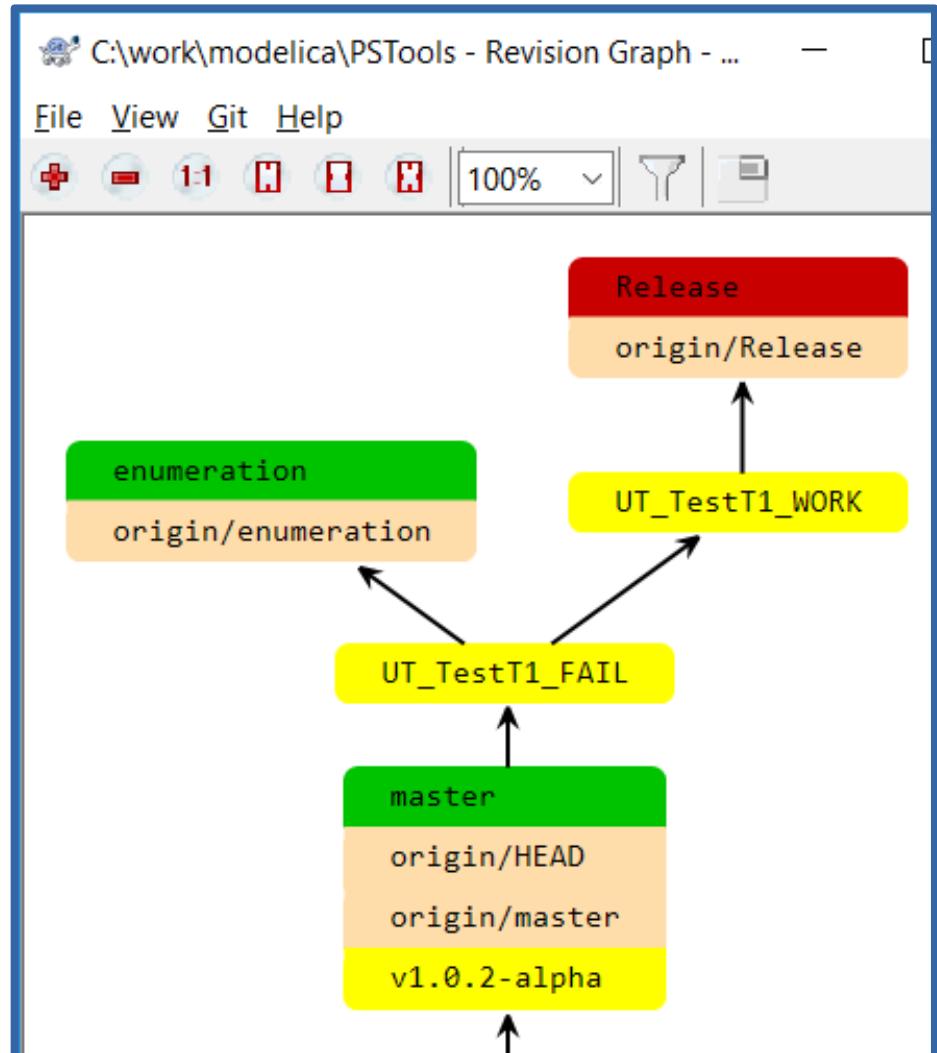


T2



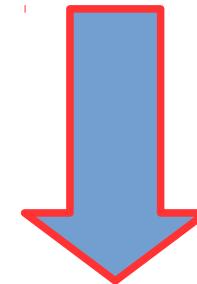
**Check**

# Case Study 1 PSTools Library



**UT\_TestT1\_FAIL**

```
// der(VS) = -qS * VX;  
g_VS[i] = -g_qS[i] * VX  
- qS * g_VX[i];
```

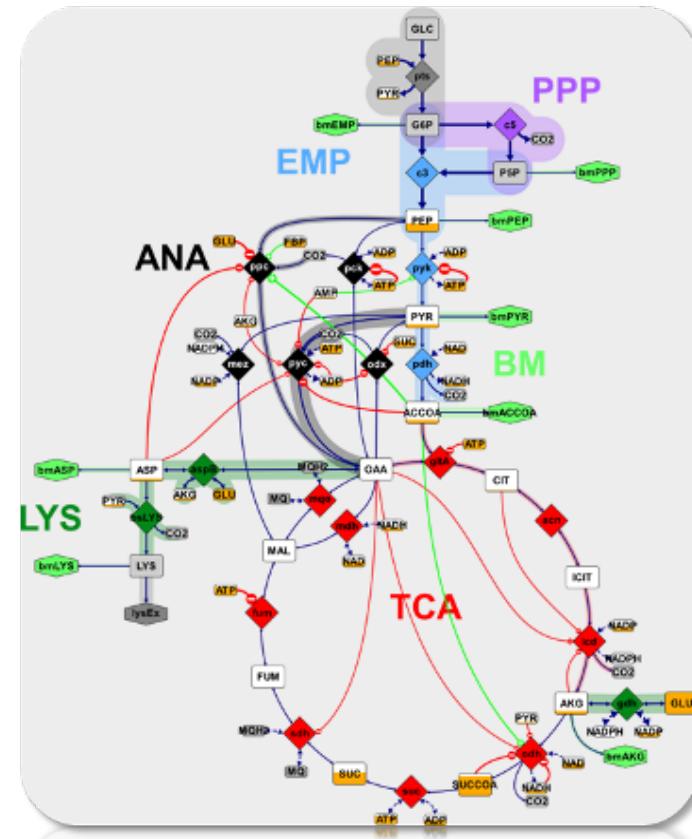
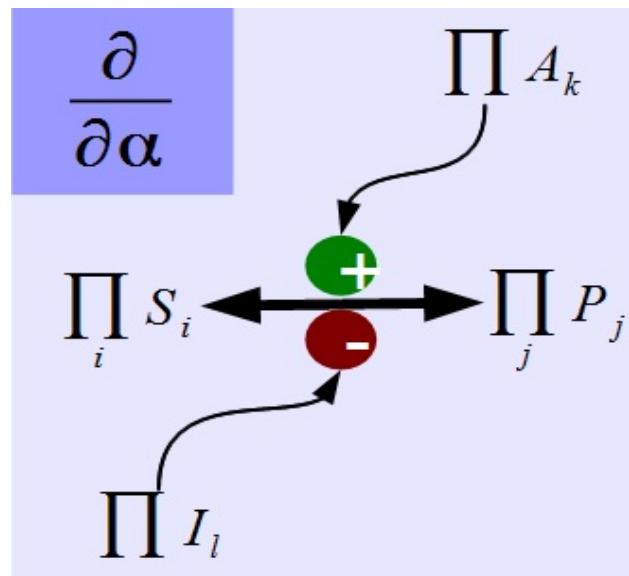


**UT\_TestT1\_WORK**

```
// der(VS) = -qS * VX;  
der(g_VS[i]) = -g_qS[i] * VX  
- qS * g_VX[i];
```

# GenKinetics

# 2018 R 1.0-alpha



$$v = \prod_a \frac{K_{A_a} + [A_a]}{K_{A_a}} \cdot \prod_b \frac{K_{I_b}}{K_{I_b} + [I_b]} \cdot \frac{V_{max}^{fwd} \prod_i \frac{[S_i]}{K_{mS_i}} - V_{max}^{bwd} \prod_j \frac{[P_j]}{K_{mP_j}}}{V_{max}^{fwd} \prod_i 1 + \frac{[S_i]}{K_{mS_i}} + V_{max}^{bwd} \prod_j 1 + \frac{[P_j]}{K_{mP_j}} - 1}$$

# Formal unit testing procedure

- 1) a unit test model for each component C using
  - Example of a small model employing C
  - Equivalent model implemented only by equations
- 2) Execute all unit tests by \*.mos & OMShell
  - after each significant modification
- 3) Investigate errors , if any

Most useful when the component checks but  
the UT does not translate or simulate

A library is shipped with its unit tests  
All unit tests are within a package called UnitTests  
Currently about 40 unit tests distributed GenKinetics

# Case Study 2 ADGenKinetics Library

OMC 1.12.0

```
A = product({KA[i] / (KA[i] + mc_A[i].c) for i in 1:NA});
```

2012



OMC 1.13.0

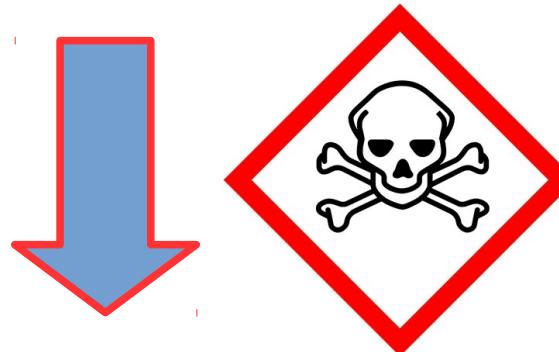
```
A = product({ (KA .+ mc_A.c) ./ KA for i in 1:NA});
```

2019

# Case Study 3 GenKinetics / Biochem Libraries

## Numerical Problem

```
der(c) = if  
          (c < tolerance) then 0 else r_net;
```

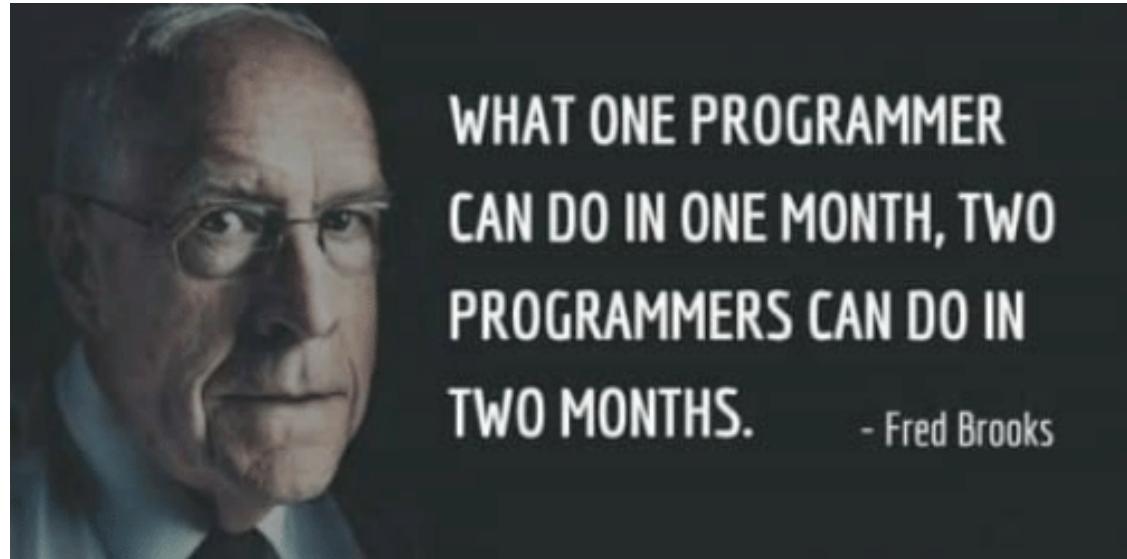


## Solution

```
der(c) = if  
          (c < tolerance and r_net < 0) then 0 else r_net;
```

# Advantages

- Simplicity
- Purely Modelica
- Suitability
  - individual developers or Modelica libraries
    - GenKinetics <https://github.com/AtiyahElsheikh/GenKinetics>
    - PSTools
  - small-scale developments
  - Minimum constraints get done
  - Shipping Unit Tests with the product



WHAT ONE PROGRAMMER  
CAN DO IN ONE MONTH, TWO  
PROGRAMMERS CAN DO IN  
TWO MONTHS.

- Fred Brooks

# Outlook

- a user experience report from GenKinetics
- Combine Relative Error w. Absolute Error

Asghar, Adeel, Andreas Pfeiffer, Arunkumar Palanisamy, Alachew Mengist,  
Martin Sjölund, Adrian Pop, and Peter Fritzson.

"Automatic Regression Testing of Simulation Models and Concept for  
Simulation of Connected FMUs in PySimulator."

*InProceedings of the 11th International Modelica Conference, Versailles.* 2015.

- Continuous Integration Solution